

# Carbon Neutrality

---

Steven Low



Caltech

NSF Workshop April 2023



# Outline

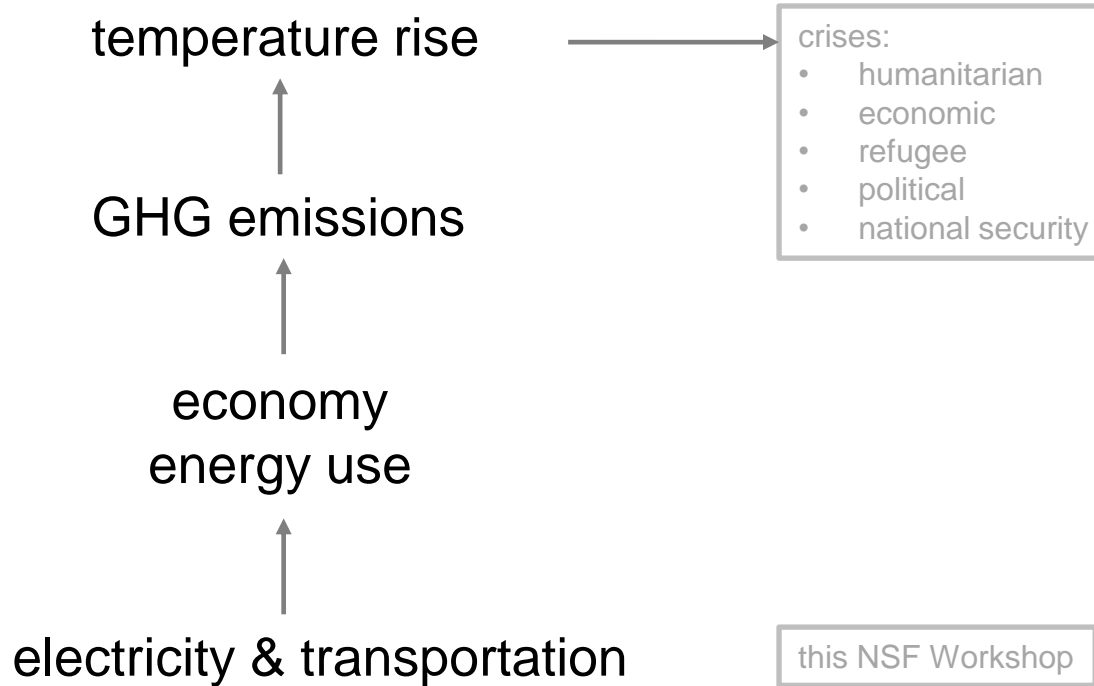
Trends and research needs (10)

Some experiences

- From EV charging (5)
- ... to workplace decarbonization (10)
- ... to unbalanced 3-phase power flows (15)

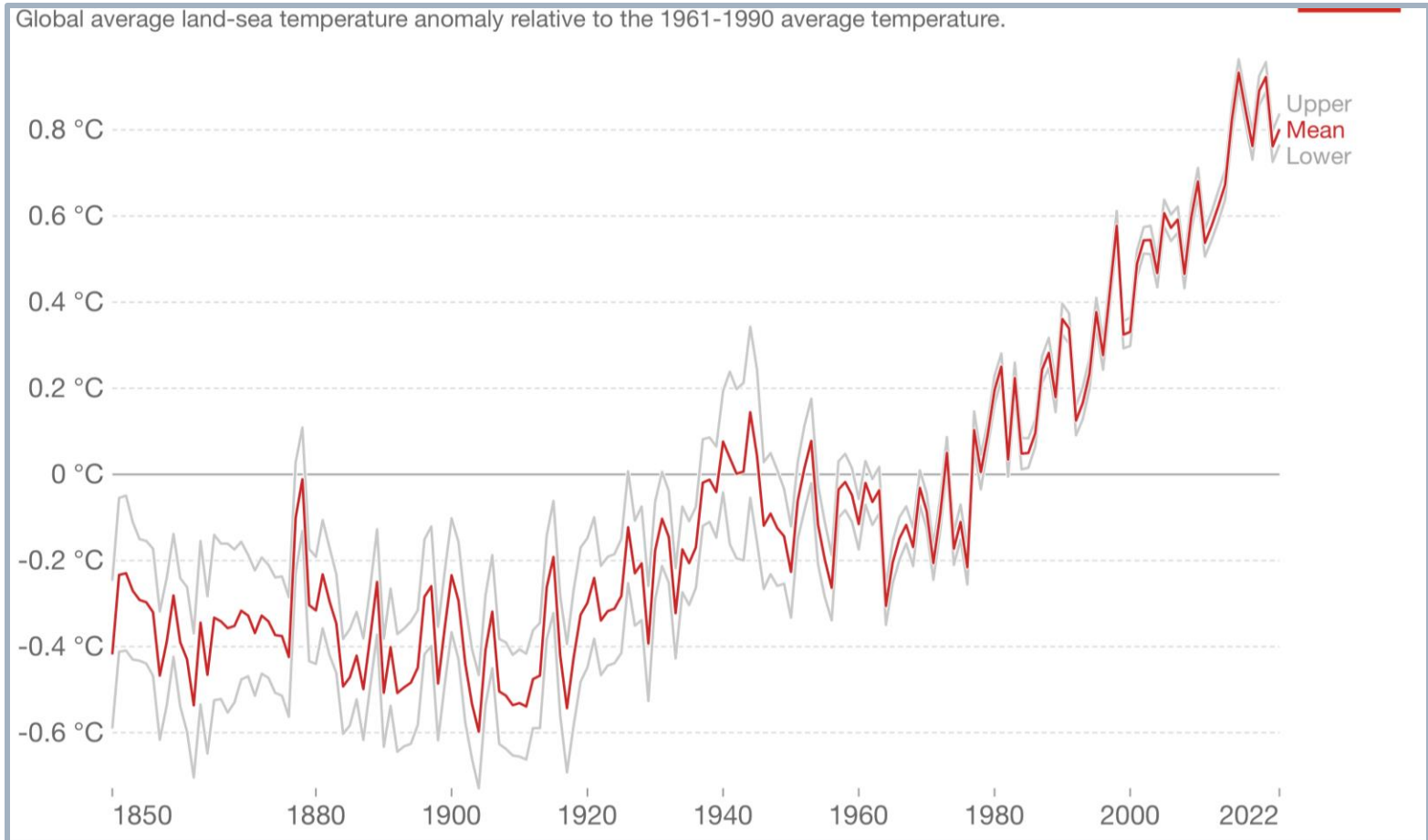


# Why this workshop





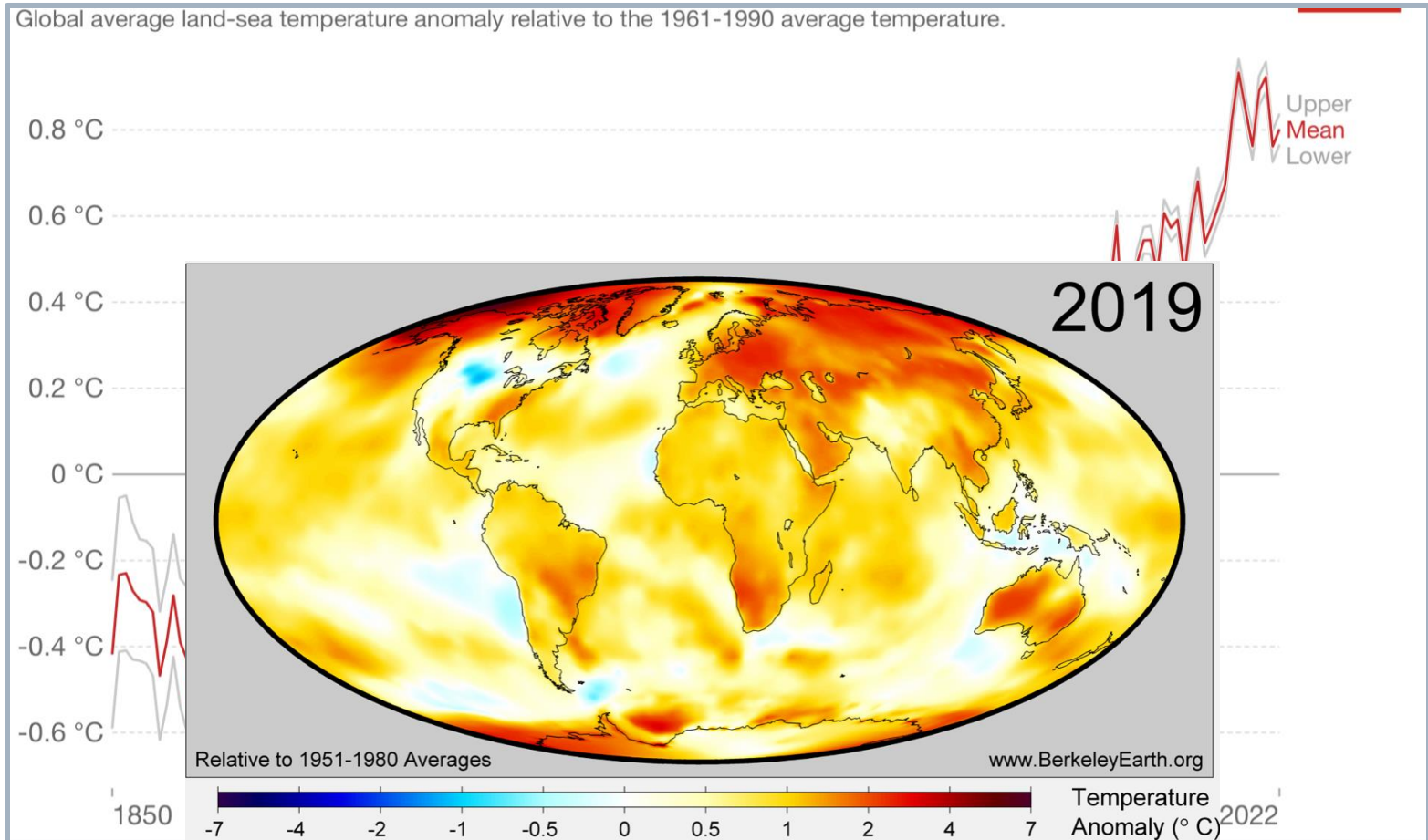
# Average temperature



Global average temp has increased by  $>1^{\circ}\text{C}$  since pre-industrial time



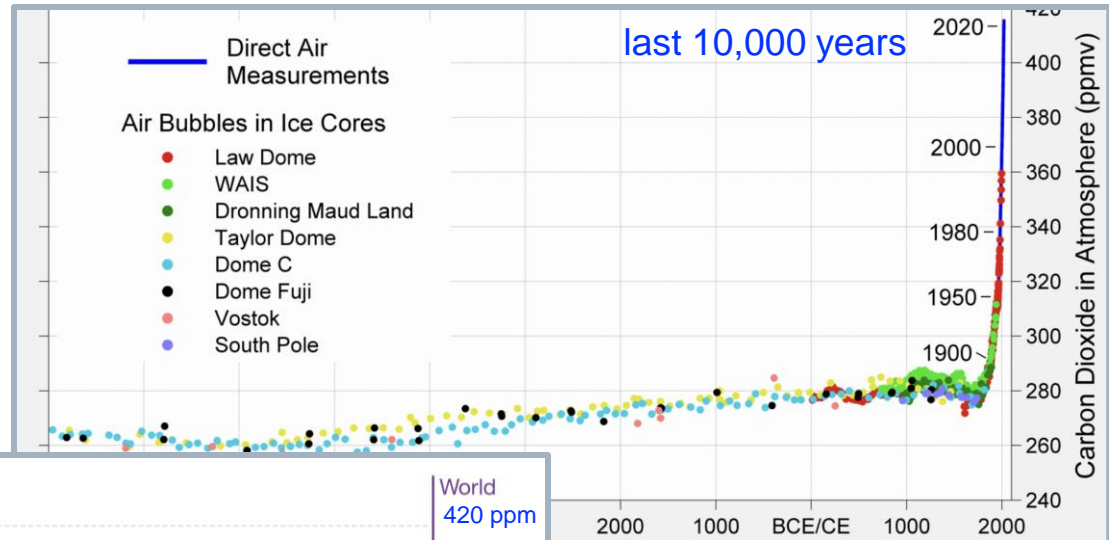
# Average temperature



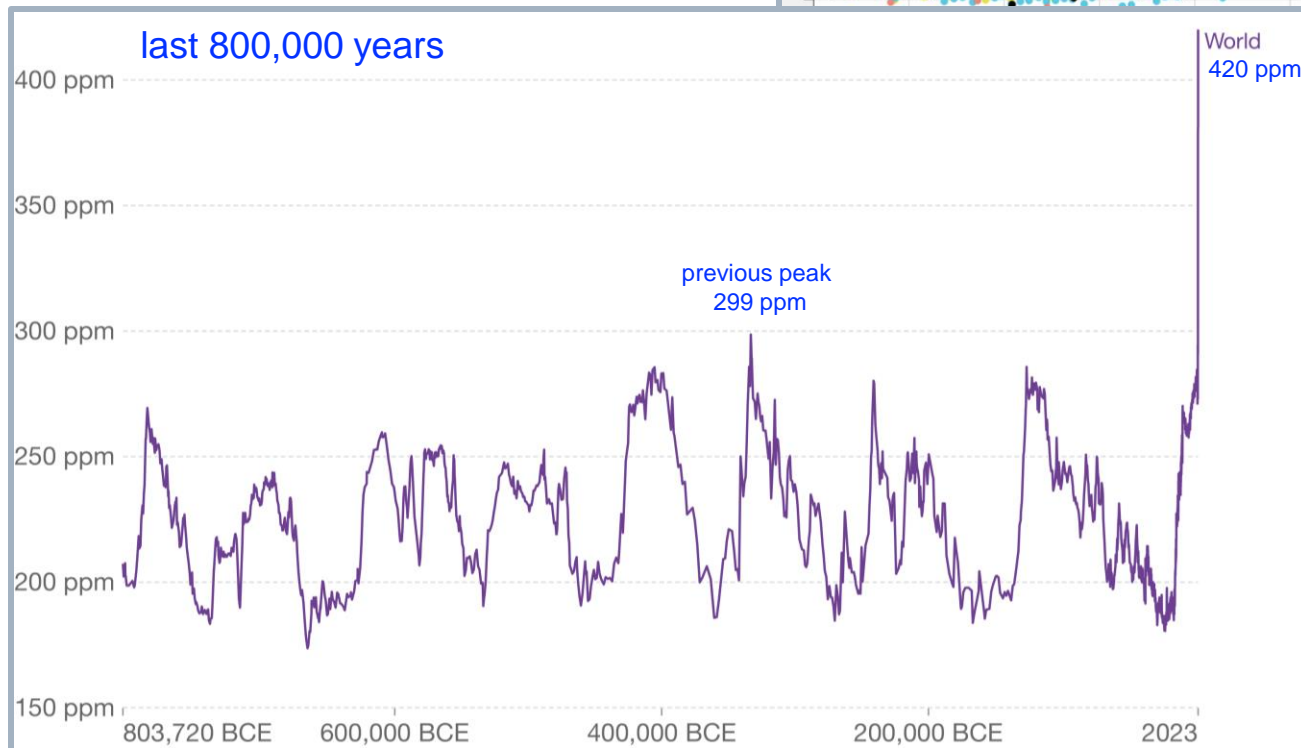
Local temperature can be much warmer than global average



# Atmospheric CO<sub>2</sub>

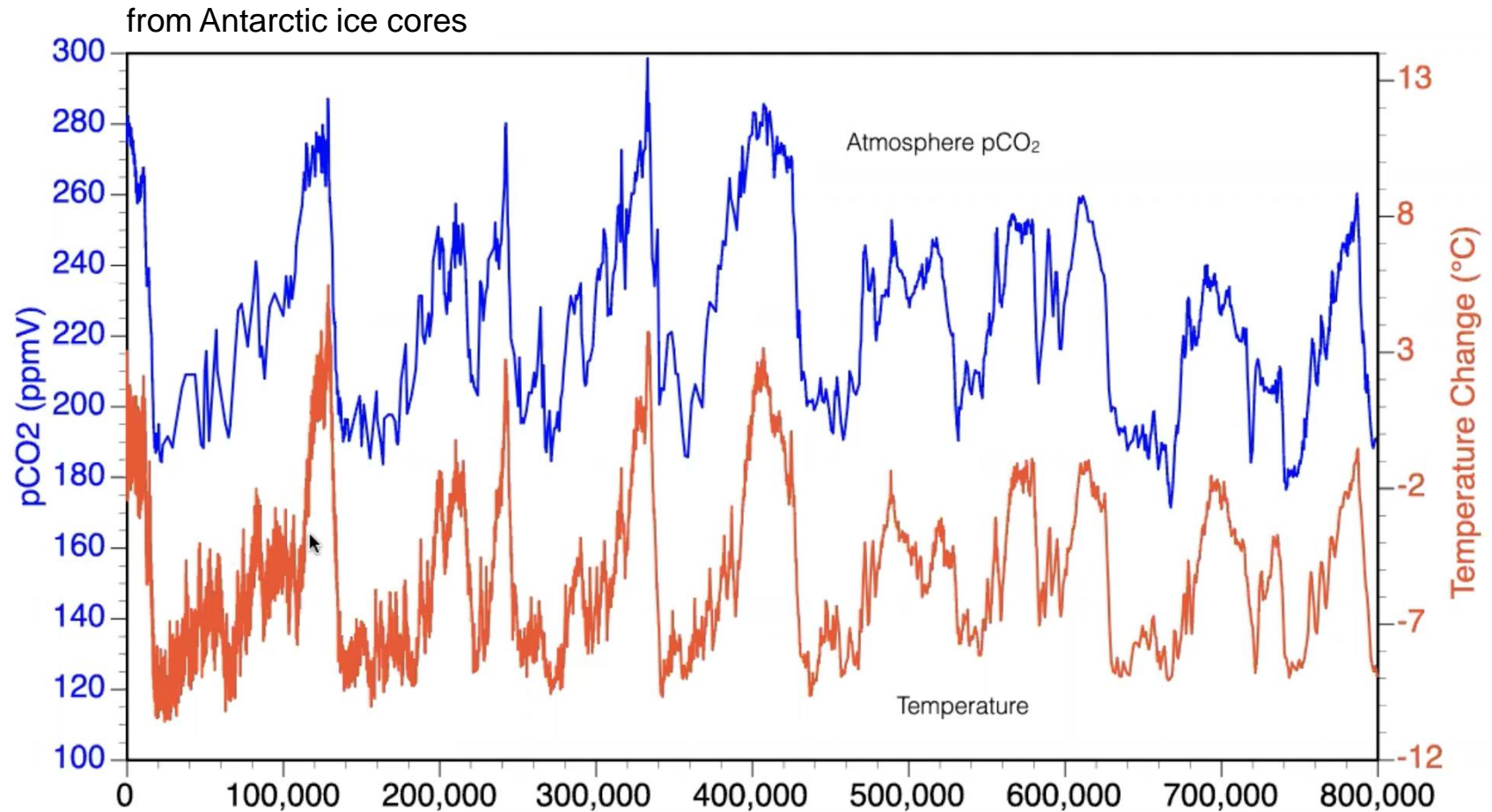


[berkeleyearth.org/dv/10000-years-of-carbon-dioxide/](https://berkeleyearth.org/dv/10000-years-of-carbon-dioxide/)



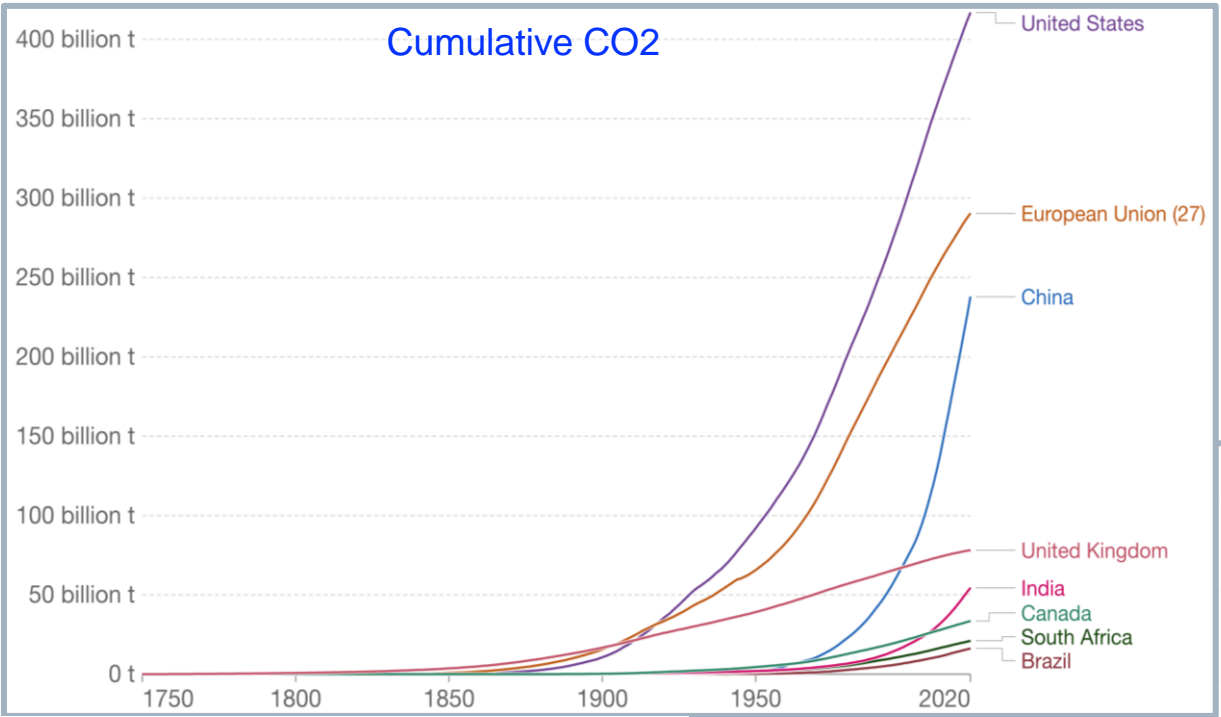


# CO<sub>2</sub> and temperature

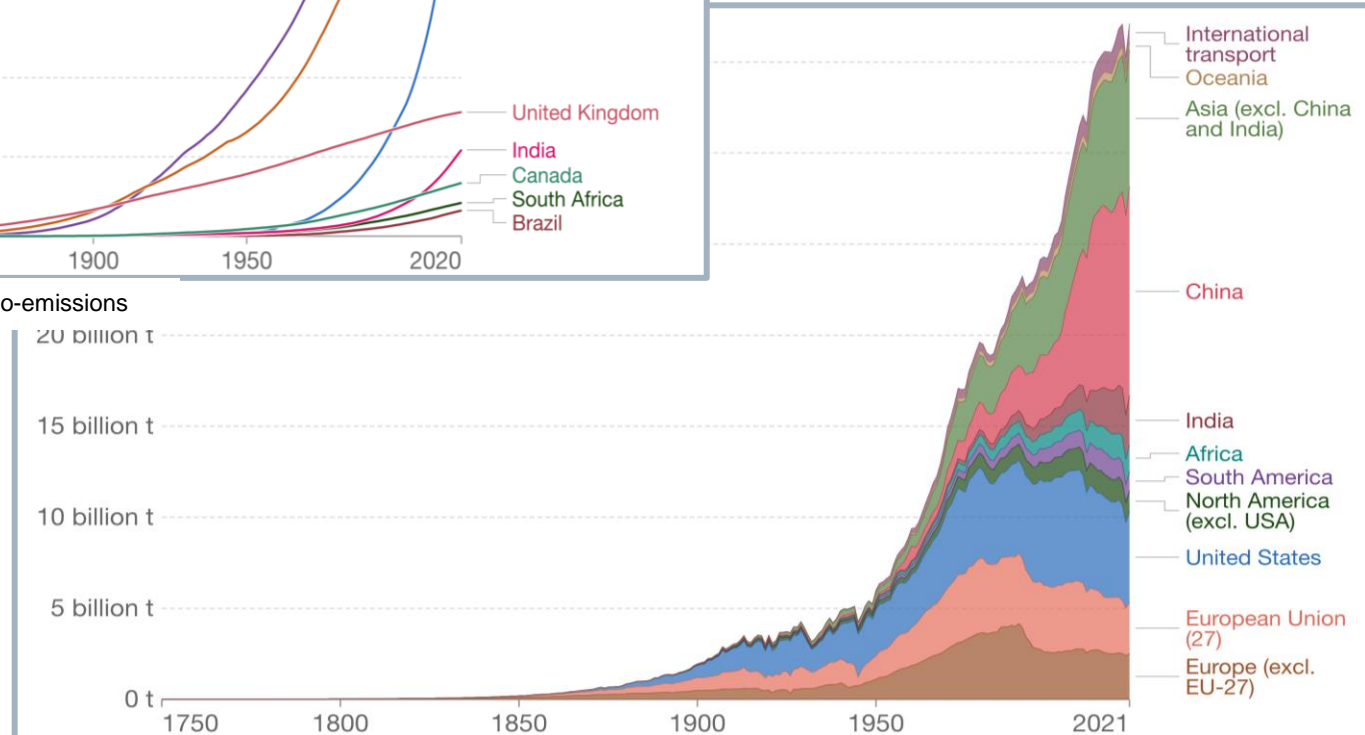




# CO2 emissions



<https://ourworldindata.org/grapher/cumulative-co-emissions>

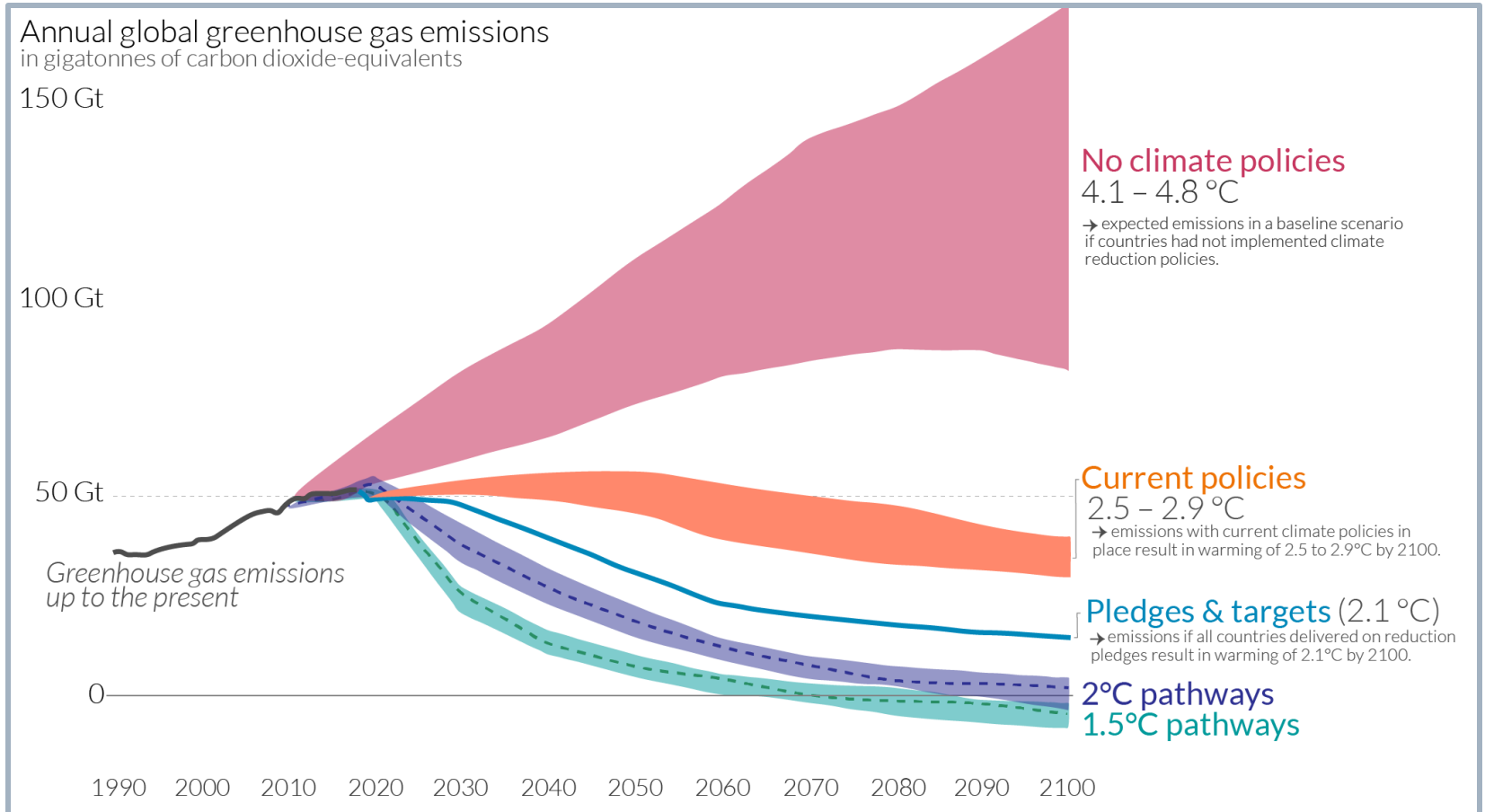


<https://ourworldindata.org/co2-and-greenhouse-gas-emissions>



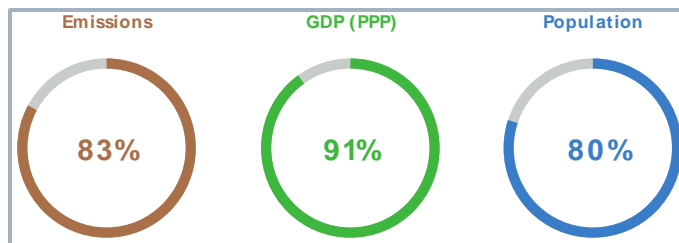
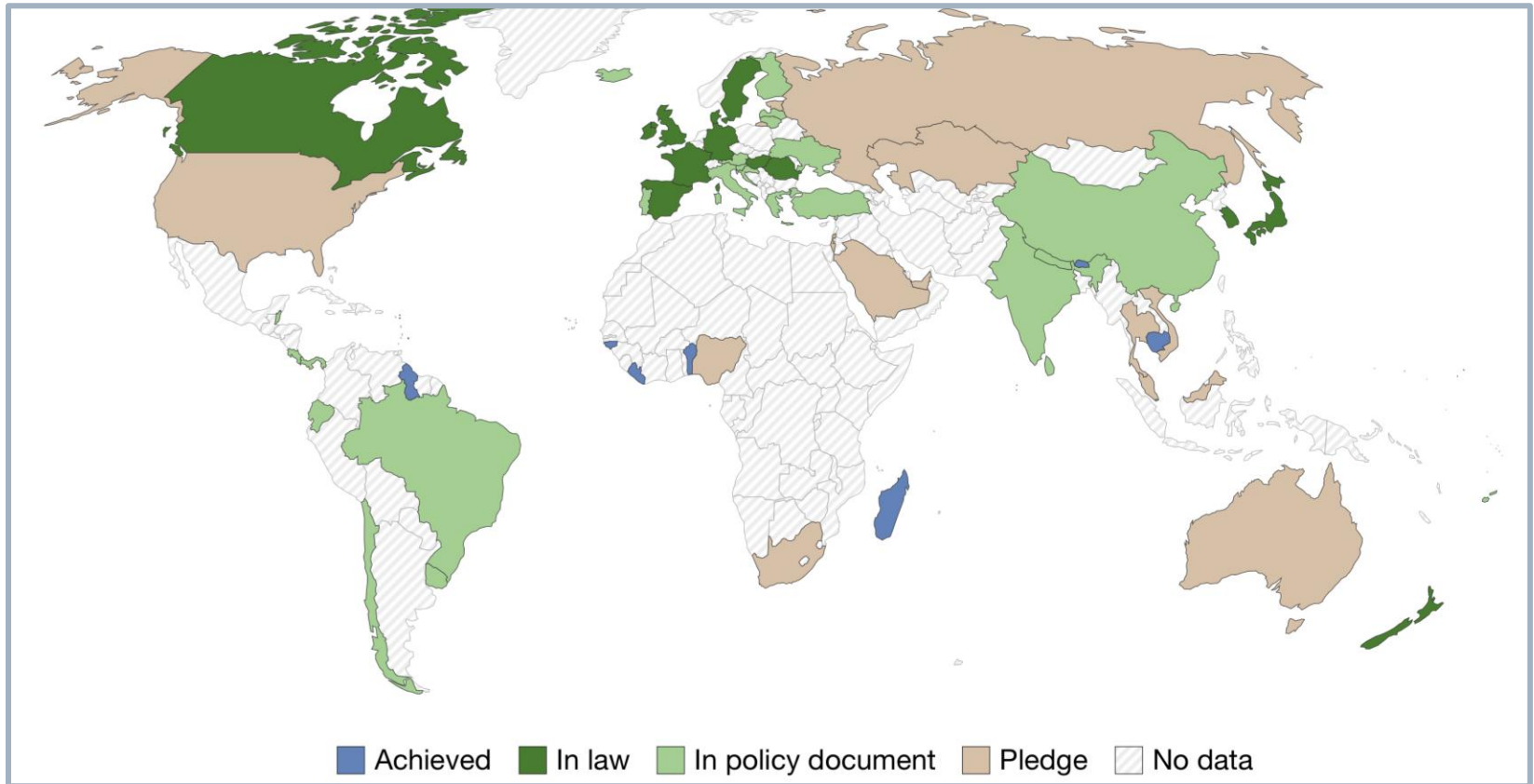


# GHG pathways





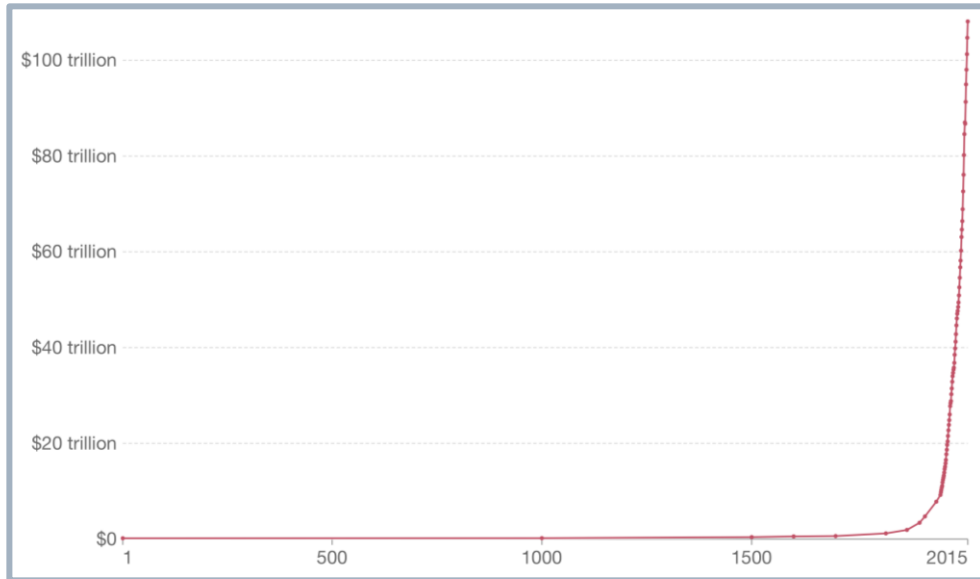
# Net zero GHG pledges



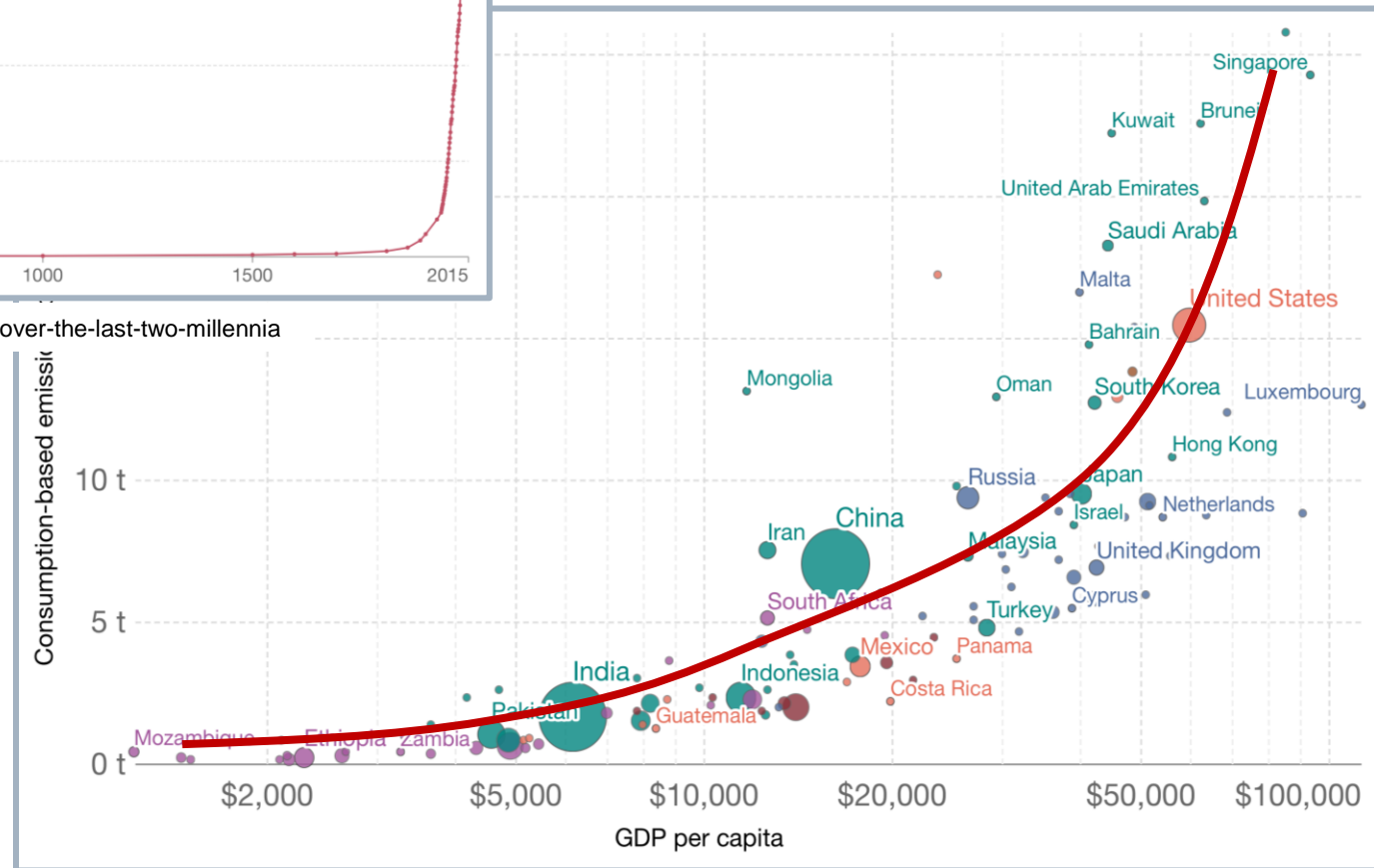
% coverage of net zero GHG pledges (Oxford 2022)  
(2019: coverage = 16% GDP)



# CO2 and GDP



<https://ourworldindata.org/grapher/world-gdp-over-the-last-two-millennia>

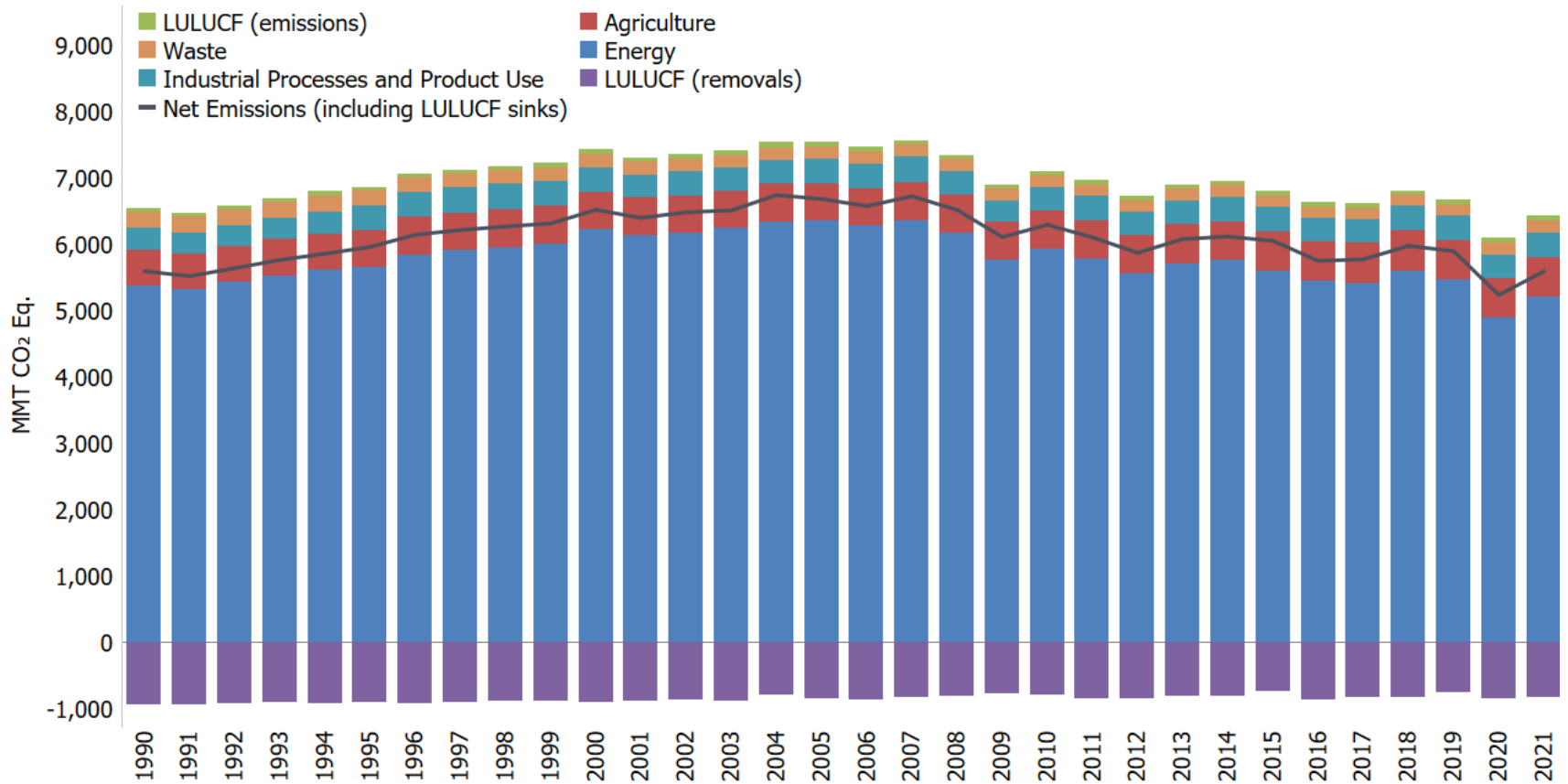


x-axis is not time:  
energy inequality

<https://ourworldindata.org/grapher/consumption-co2-per-capita-vs-gdppc>



# GHG and energy use

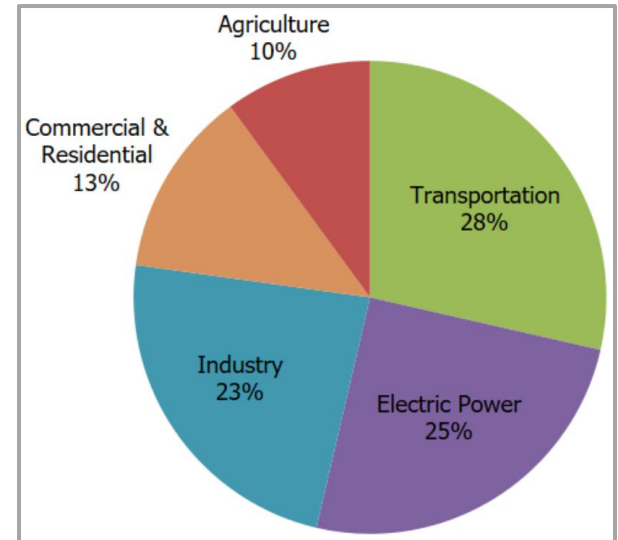
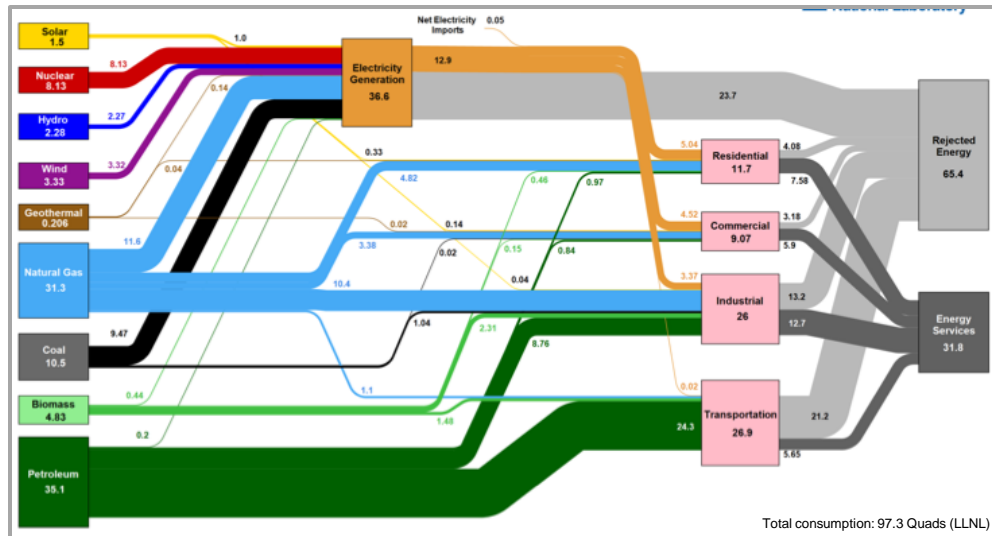


Energy use emitted 82% of total greenhouse gas emissions in US in 2021 (EPA)



# Electricity gen & transportation

2021 consumption: fossil 79.0%; renewables 12.5% (US EPA)



[https://flowcharts.llnl.gov/sites/flowcharts/files/2022-09/Energy\\_2021\\_United-States.pdf](https://flowcharts.llnl.gov/sites/flowcharts/files/2022-09/Energy_2021_United-States.pdf)

<https://www.epa.gov/ghgemissions/sources-greenhouse-gas-emissions#transportation>

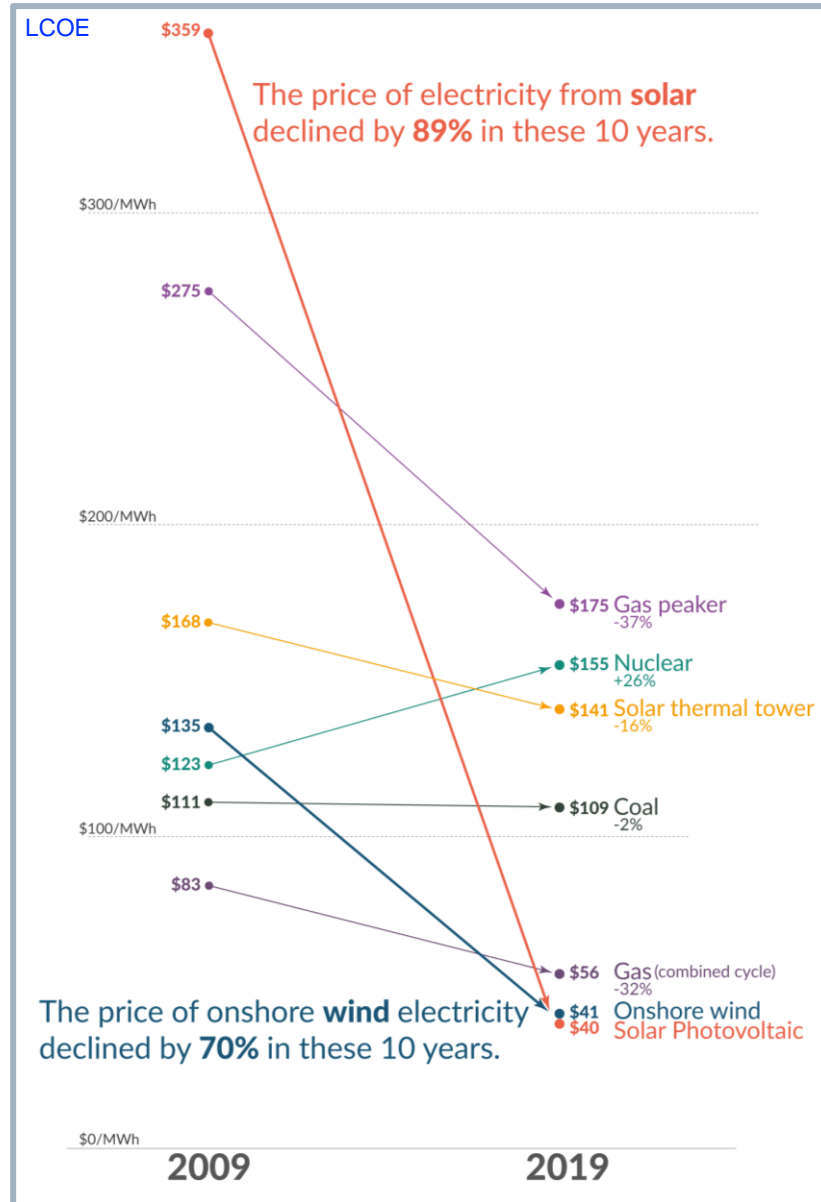
## Electricity generation & transportation in US:

- Consume 65% of all energies in 2021 (US EPA)
- Emit 53% of all greenhouse gases in 2021 (US EPA)

both numbers are lower than 2019 numbers by only ~2% !



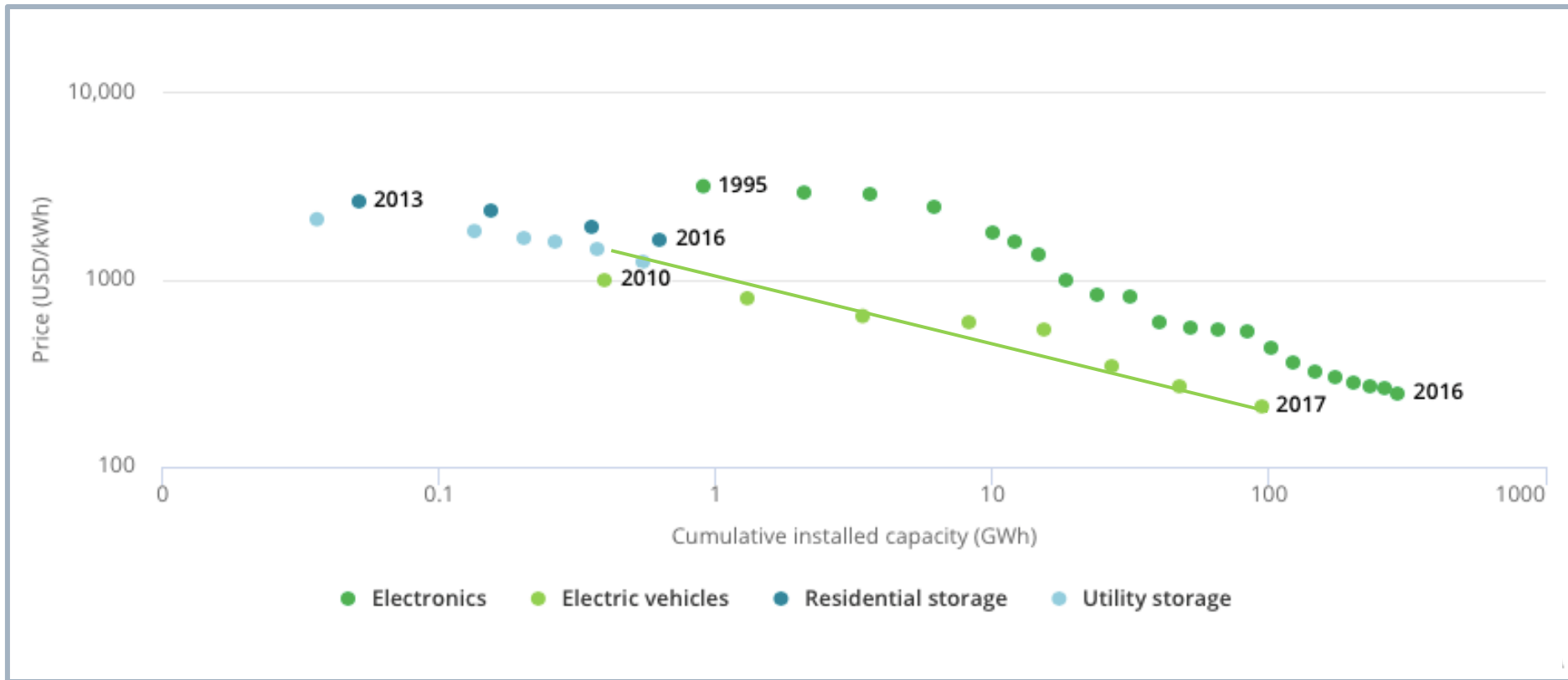
# Electricity cost



PV & on-shore wind have lowest LCOE



# Li-ion battery cost



## Electric vehicle battery:

- 2010: \$1,000 / kWh
- 2016: \$ 275 / kWh
- 2030e: \$ 73 / kWh (Bloomberg New Energy Finance 2016)



# Some challenges

Numerous research needs/opportunities

- Many experts in this NSF Workshop !





# Some challenges

## Integration of grid & mobility

Panel 1

- Technologies, economics, deployment

## Data, learning, control

Panels 2, 4

- Unknown/unreliable models, uncertainty, scalability, multiple timescales, reliability

## Equitable development

Panel 3

- Per capita CO<sub>2</sub>(consumption): US(15.5t) vs Mexico(3.4t), AU(13.8t) vs Indonesia(2.3t), Switzerland(12.4t) vs Portugal(4.7t) (D. Kammen)

## Inverter-based resources

- Dynamics, stability, scalability

## Economics & policies

- NEM: PV+EV charging+storage, aggregation; hosting cap. (L. Tong)

## Architecture

- Layering, constraints that deconstrain, RYF [John Doyle, Caltech]



# Outline

Trends and research needs (10)

## Some experiences

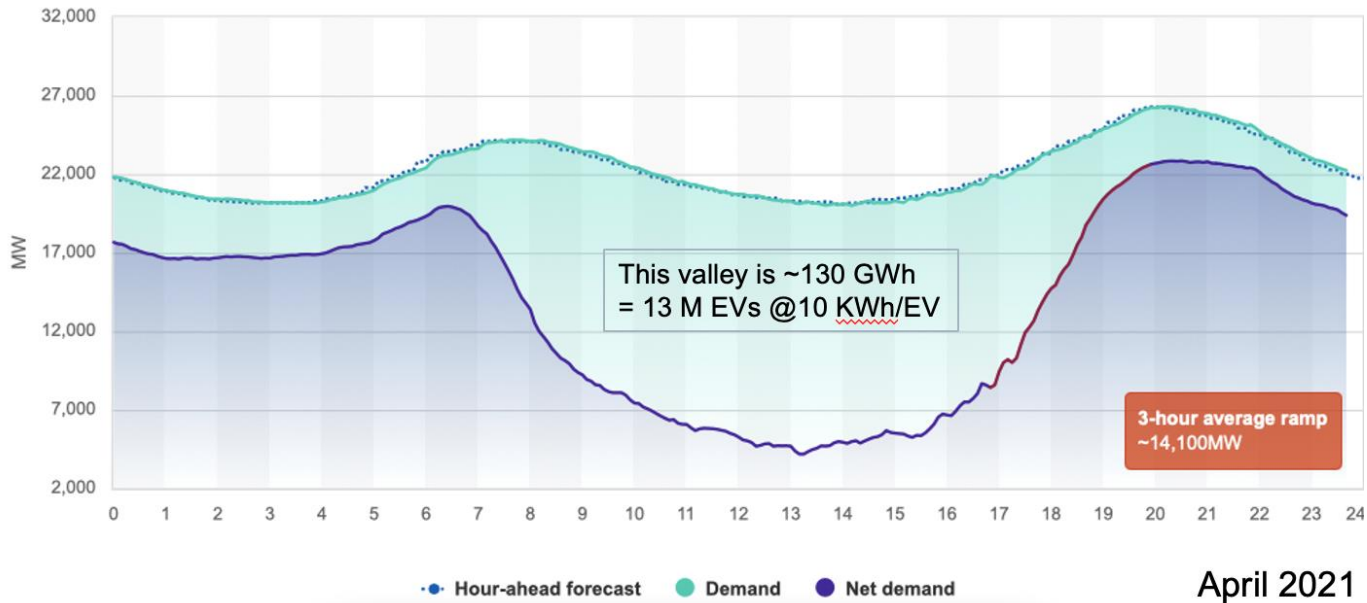
- From EV charging (5)
- ... to workplace decarbonization (10)
- ... to unbalanced 3-phase power flows (15)



# Workplace charging

## CA commitment

- ~~50%~~ <sup>60%</sup> renewables by 2030, 100% by 2045
- 1.5M ZEV by 2025, 5M by 2030 (CA has ~15M cars)



**Drivers twice as likely to get EV when workplace charging is available**

(EDF Renewables survey Feb 2018)

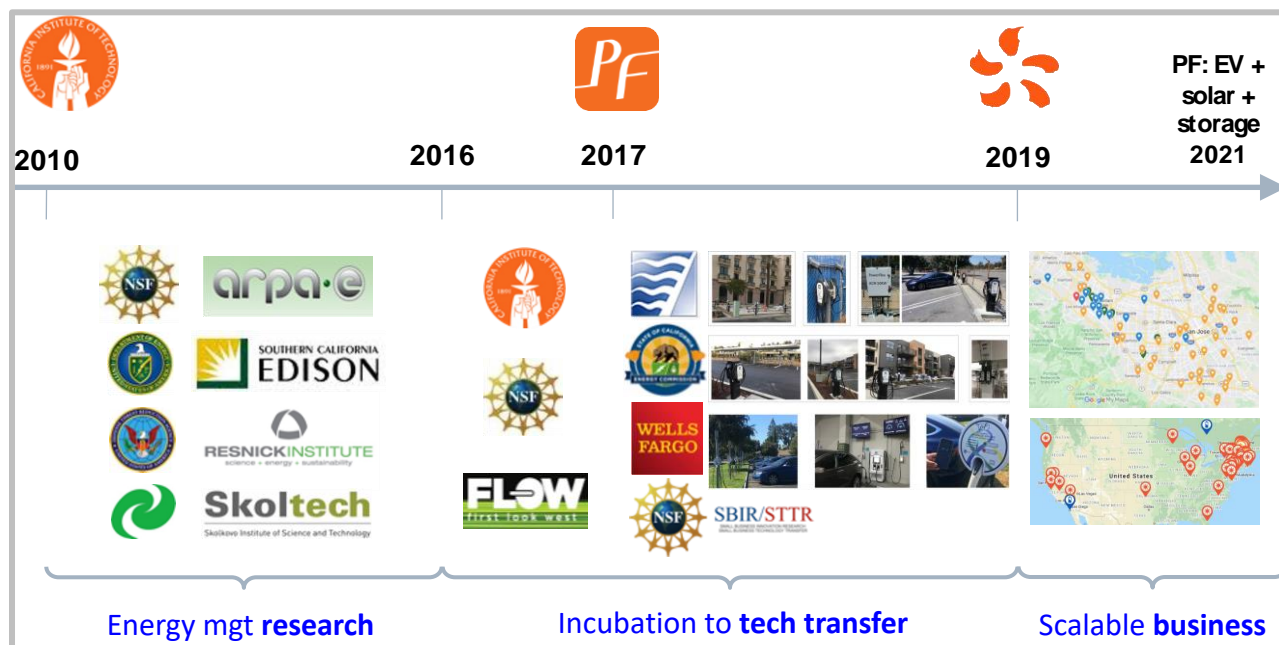


# EV charging: research → impact

## Theory and algorithms

1. **Broad power systems research (since 2010)**  
Nonconvex optimization, control & dynamical systems, distributed real-time algorithms
2. **Application to EV charging**  
Optimal decentralized protocol for EV charging (IEEE Trans. Power Systems, 2013)  
**Theorem:** Online LP attains offline optimal (IEEE PES General Meeting, 2017)

Industry	Online LP	Theoret. max
28%	53%	54%





# EV charging: research → impact

## Testbed → deployment

### 3. First pilot: Caltech garage (2016)

By July 2020: delivered 3M+ electric miles, avoided 1,000 tons of CO2e

### 4. Caltech startup: PowerFlex (2017)

Value proposition: Enable large-scale EV charging by reducing capital & operating costs  
Acquired by EDF Renewables to scale business



debugging



charger



transformer & subpanels



main panel



G. Lee (Co-founder)

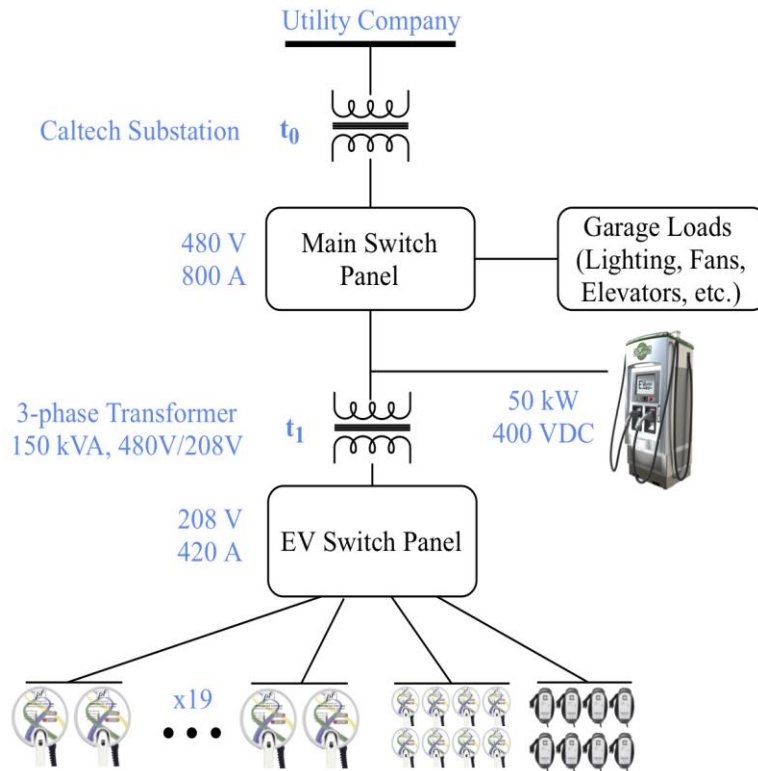


<b>Municipal</b> PASADENA SAN JOSE UNIVERSITY OF CALIFORNIA	<b>Real Estate</b> CUSHMAN & WAKEFIELD AVISON YOUNG Hines SUMMER HILL	<b>Universities</b> Caltech UC SF UC San Diego	<b>OEM</b> VW Audi Mercedes-Benz Volvo
<b>Non-profit</b> Children's Hospital Los Angeles LACMA Getty NATURAL HISTORY MUSEUM LOS ANGELES LGBT CENTER	<b>Research</b> NREL SLAC JPL	<b>Workplace</b> Intuit SAP Adobe 23andMe	<b>Medium-duty Fleet</b> DHL UPS





# Caltech ACN: physical system







# Caltech ACN: cyber system

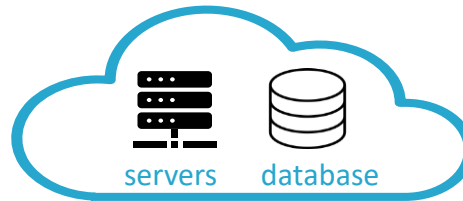
Model predictive control: QCQP

$$\begin{aligned} \max_r \quad & \sum_v \alpha_v u_v(r) \\ \text{s.t.} \quad & 0 \leq r_i(t) \leq \bar{r}_i(t) \\ & \sum_{t \in T} r_i(t) \leq e_i \\ & \left| \sum_{i \in V} A_{ti} r_i(t) e^{j\phi_i} \right| \leq c_{lt}(t) \end{aligned}$$

Highly customizable QCQP

- objectives: cost, PV, asap, regularization
- constraints: energy, deadlines, capacities
- determine charging rates for all EVs

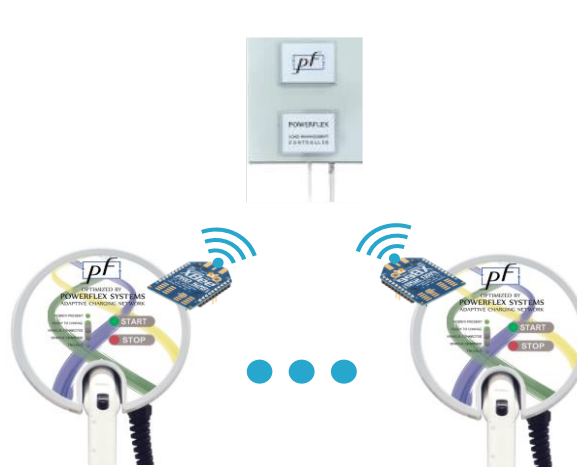
PF cloud



IP/cellular



Garage

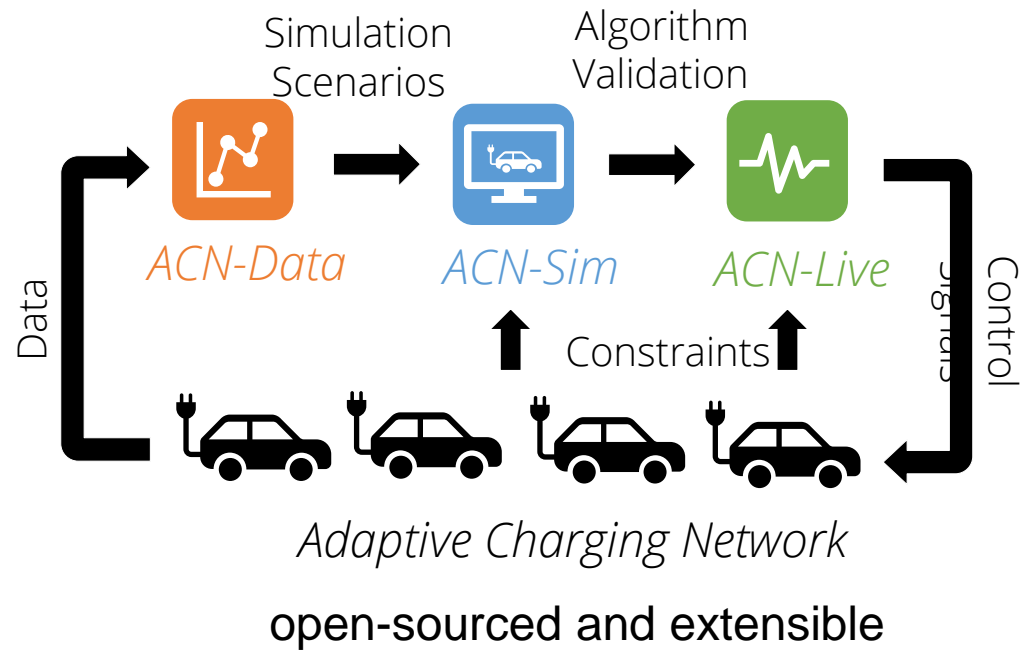


Mobile app



# Caltech ACN: open research tool

- ACN-Data
- ACN-Sim
- ACN-Live (HW-in-the-loop)



Lee, Li, Low. ACN-Data: analysis and applications of an open EV charging Dataset  
ACM e-Energy, June 2019

Lee, Johansson, Low. ACN-Sim: an open-source simulator for data-driven EV charging research  
IEEE SmartGridComm, October 2019





# ACN research portal

Adaptive Charging Network

HOME INFO RESEARCH DATA SIMULATOR ACCOUNT ▾

## The Adaptive Charging Network

Accelerating Electric Vehicle Research @ Caltech and Beyond

Zach Lee  
zlee@powerflex.com



[ev.caltech.edu](http://ev.caltech.edu)



# Lessons learnt

## Smart EV charging

- R&D to extract **untapped** value intrinsic to EV charging
- Critical to maintain broad theory research
- Translation of energy R&D is hard

## Workplace energy systems

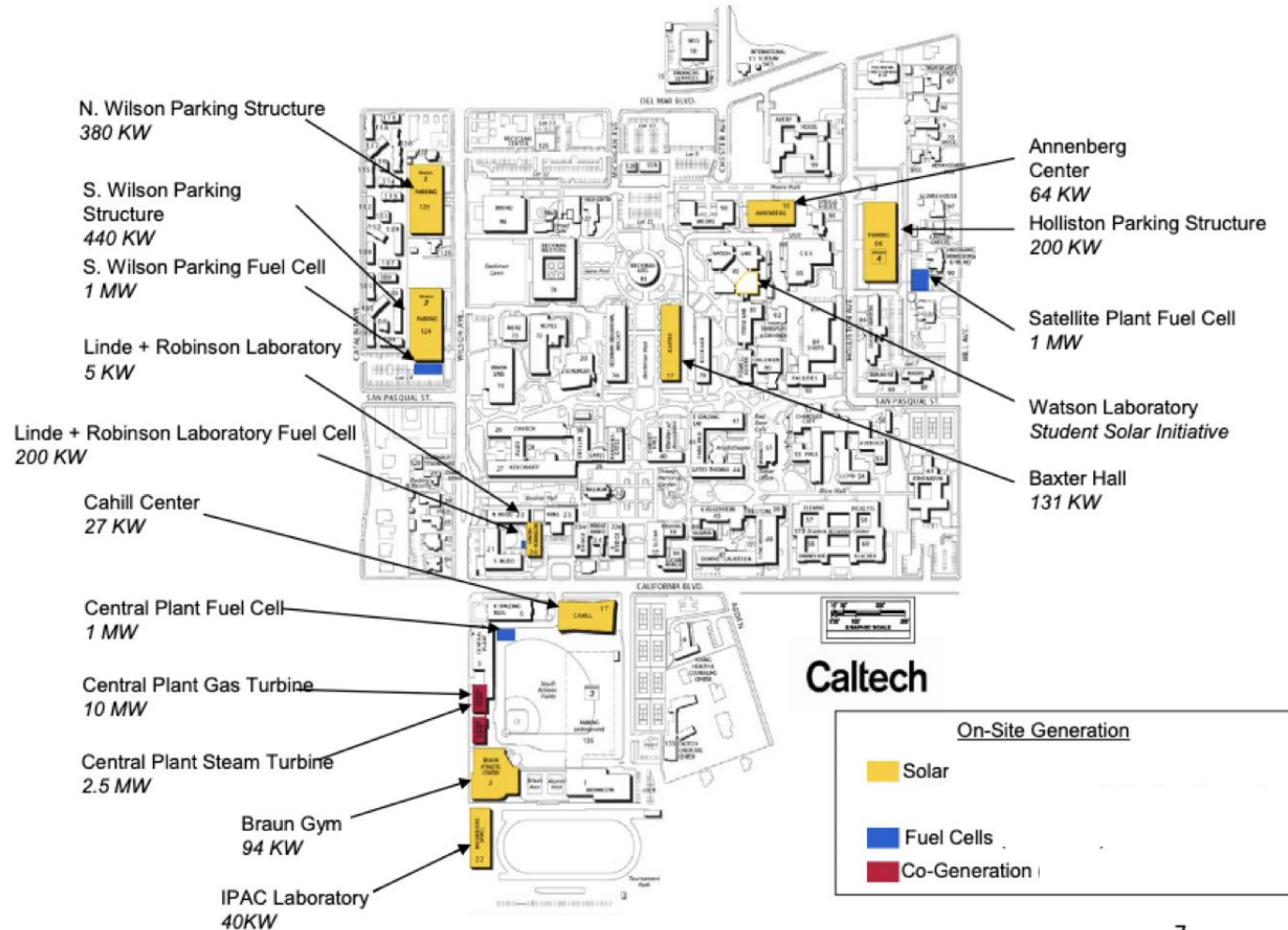
- Large **untapped** value in current system
- Bigger & more complicated system, more expensive infrastructure, more difficult & diverse technical challenges



# Caltech energy systems

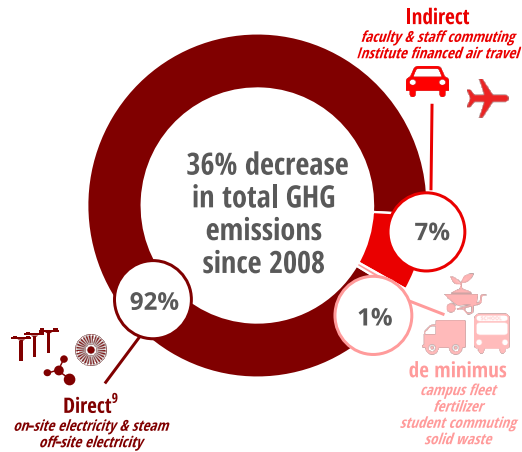
## Caltech microgrid

- ~200,000-people city
- >100 commercial-size buildings
- 3 grid interconnections
- 4 substations
- 20 MW peak load
- 2.1 MW onsite solar
- 4 MW NG fuel cells
- 12.5 MW gas co-gen
- Chilled water distribution
- Fossil-based steam and HW distribution

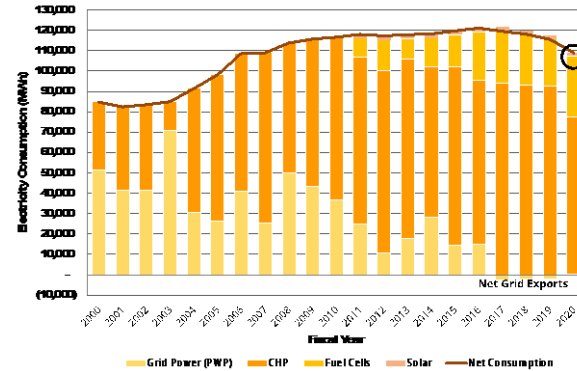




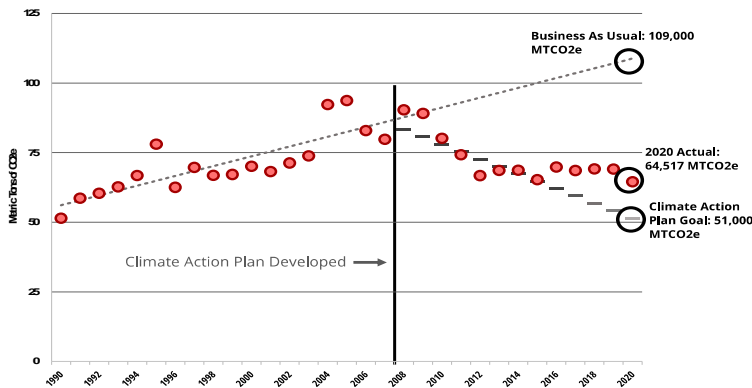
# Opportunities



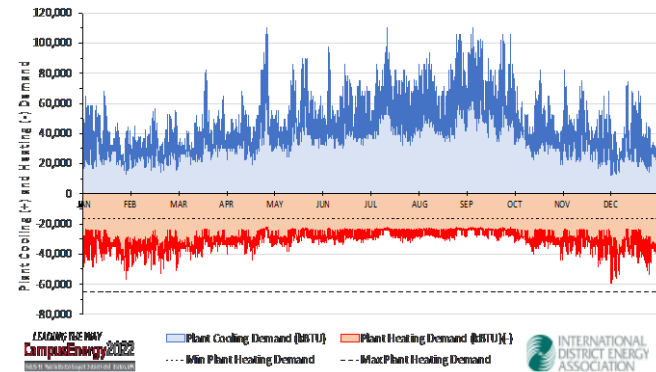
Energy is a 92%-opportunity to reduce GHG



Co-gen generated 78% of electricity consumed in 2020



Further reduction needs to retire campus co-gen



Simultaneous heating and cooling demands



# Basic idea

Integrate and holistically optimize operation of electric, heating & cooling systems

- They operate independently today
- HRCs to provide **net** heating & cooling demand

Exploit storage (batteries & thermal) and HRCs to shape electricity demand

- To adapt to random fluctuations in demand, prices & CO<sub>2</sub> intensity
- Greatly reduces capital and operating costs for 24/7 CO<sub>2</sub> neutrality



# Campus decarbonization

## Infrastructure ([Caltech Admin/Facilities](#))

- Retiring co-gen, electrify hot & chilled water, HRCs, thermal storage, batteries, tunnels & pipes

## Data ([Caltech testbed](#))

- Comprehensive reliable data on electric, cooling & heating systems, cost & emission data

## Theory, algorithms & prototypes ([focus of R&D](#))

- Theory & algorithms for real-time learning, control & optimization of DERs
- Software prototypes (Digital Twin)

## Pilot & deployment

- Work with Caltech Facilities
- Work with industry



# R&D: theory, algorithms, prototypes

Layer	R&D	Open problems (examples)
<b>Control</b>	Optimization-based decision making for planning and operation in uncertainty	• Data-driven stochastic optimization • Data-driven real-time OPF
<b>Learning</b> (Digital Twin)	Data-driven continuous learning, identification & tracking of system models & current states	
<b>Data</b> (Meter Caltech)	Testbed to provide real-time comprehensive & reliable data	

## Expected outcomes:

- DER live testbed: PV, building, EV, storage, monitoring system (meters & software)
- Theory & algorithms for learning, control, and optimization of networked DERs
- Software prototypes of some algorithms

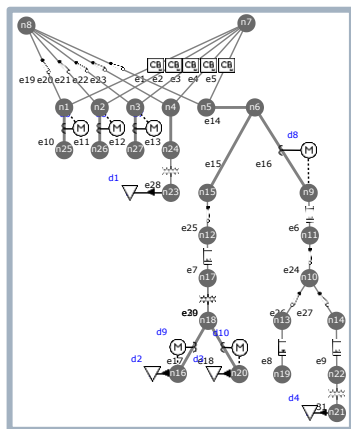
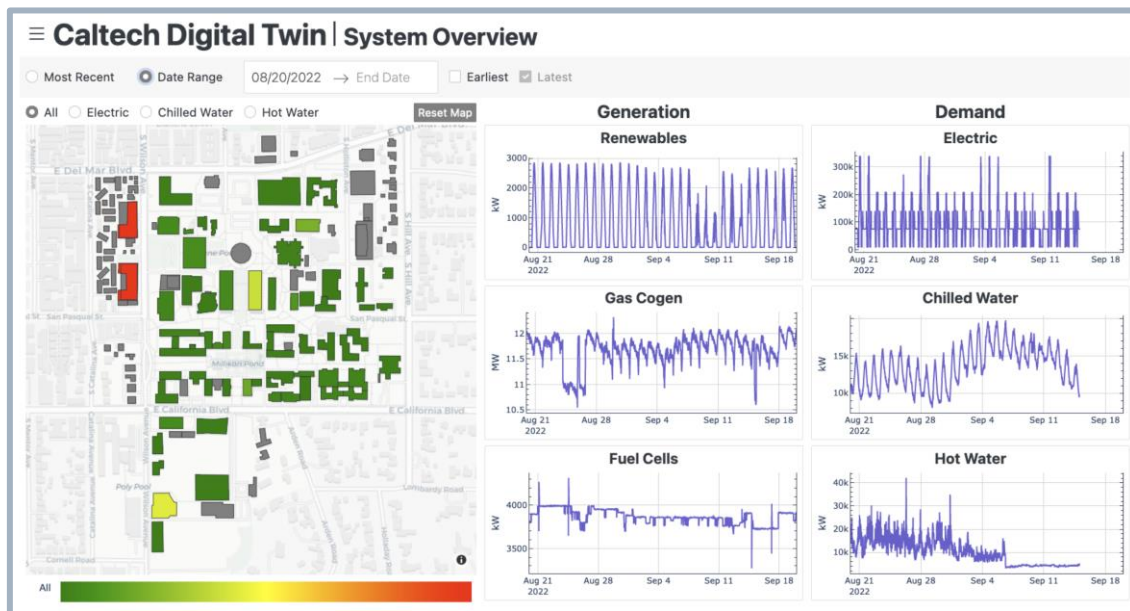
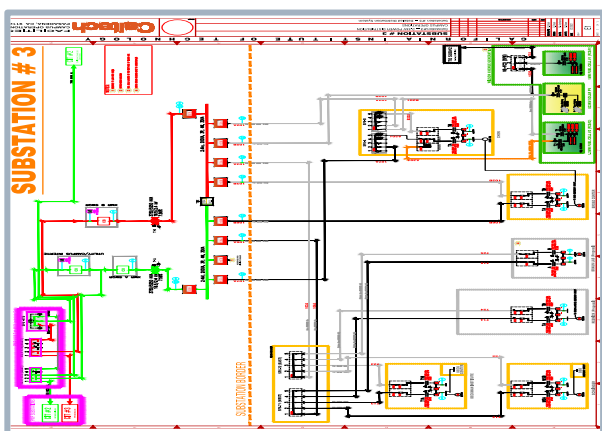




# DER testbed

## Substation 3 (16.5kV/2.4kV/480V)

- Buildings
- Rooftop PVs
- Fuel cells
- EV chargers



digital circuit diagram



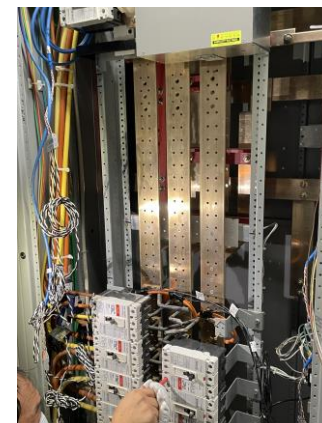
electric room



metering cabinet



meters, CTs



3p voltage taps





# Network identification

$$I = YV \text{ where } Y_{jk} = \begin{cases} -y_{jk}^s, & j \sim k \ (j \neq k) \\ \sum_{l:j \sim l} y_{jl}^s, & j = k \\ 0 & \text{otherwise} \end{cases}$$

$Y$  is a complex symmetric (Laplacian) matrix with zero row sums

## Learning $Y$ from data

- Numerous control & optimization schemes assume  $Y$  is known
- But  $Y$  often unavailable or unreliable in **distribution** systems (e.g., Caltech does not know  $Y$ )
- Little is known about analytical properties of  $Y$  (e.g., invertibility only published in [Yuan et al 2022, Torizo & Molzahn 2022, Low 2022])

## State of the art

- Full measurement: many schemes based on regressions, entropy, sparse recovery, graph processing, ...
- With hidden nodes (for **radial** networks) ?



# Network identification with hidden nodes

At each time  $t$  :

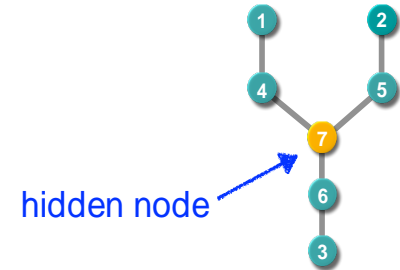
$$\begin{array}{l}
 \text{0 injection} \\
 \text{at hidden node} \rightarrow
 \end{array}
 \begin{bmatrix} I_1(t) \\ 0 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} V_1(t) \\ V_2(t) \end{bmatrix}$$

$\leftarrow$  measured nodes  
 $\leftarrow$  hidden nodes

Suppose we can exactly recover  $\bar{Y}$  from  $(V_i(t), I_i(t))$  at  $i \in M$

$$I_1(t) = \bar{Y}V_1(t)$$

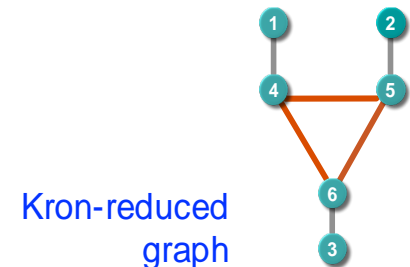
with  $\bar{Y} := Y_{11} - Y_{12}Y_{22}^{-1}Y_{12}^T$



## Lemma

Kron-reduced admittance matrix  $\bar{Y}$  exists, if lines are resistive & inductive

(Note that  $Y$  is complex symmetric !)





# Network identification with hidden nodes

At each time  $t$  :

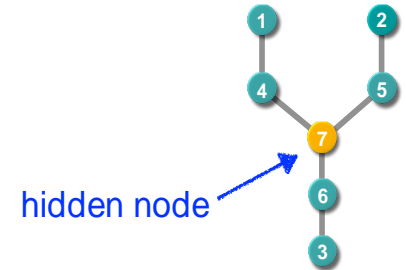
$$\begin{array}{l}
 \text{0 injection} \\
 \text{at hidden node} \rightarrow
 \end{array}
 \begin{bmatrix} I_1(t) \\ 0 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} V_1(t) \\ V_2(t) \end{bmatrix}$$

$\leftarrow$  measured nodes  
 $\leftarrow$  hidden nodes

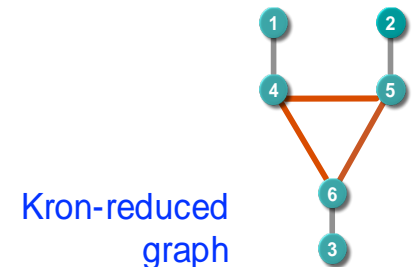
Suppose we can exactly recover  $\bar{Y}$  from  $(V_i(t), I_i(t))$  at  $i \in M$

$$I_1(t) = \bar{Y}V_1(t)$$

with  $\bar{Y} := Y_{11} - Y_{12}Y_{22}^{-1}Y_{12}^T$



Can we identify  $Y$  from  $\bar{Y}$  for radial networks ?





# Network identification with hidden nodes

At each time  $t$  :

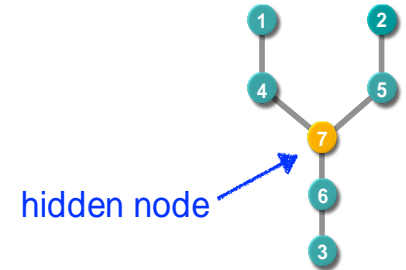
$$\begin{array}{l}
 \text{0 injection} \\
 \text{at hidden node} \rightarrow
 \end{array}
 \begin{bmatrix} I_1(t) \\ 0 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} V_1(t) \\ V_2(t) \end{bmatrix}$$

$\leftarrow$  measured nodes  
 $\leftarrow$  hidden nodes

Suppose we can exactly recover  $\bar{Y}$  from  $(V_i(t), I_i(t))$  at  $i \in M$

$$I_1(t) = \bar{Y}V_1(t)$$

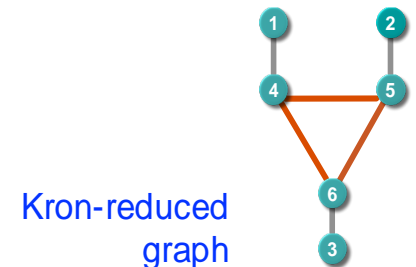
with  $\bar{Y} := Y_{11} - Y_{12}Y_{22}^{-1}Y_{12}^T$



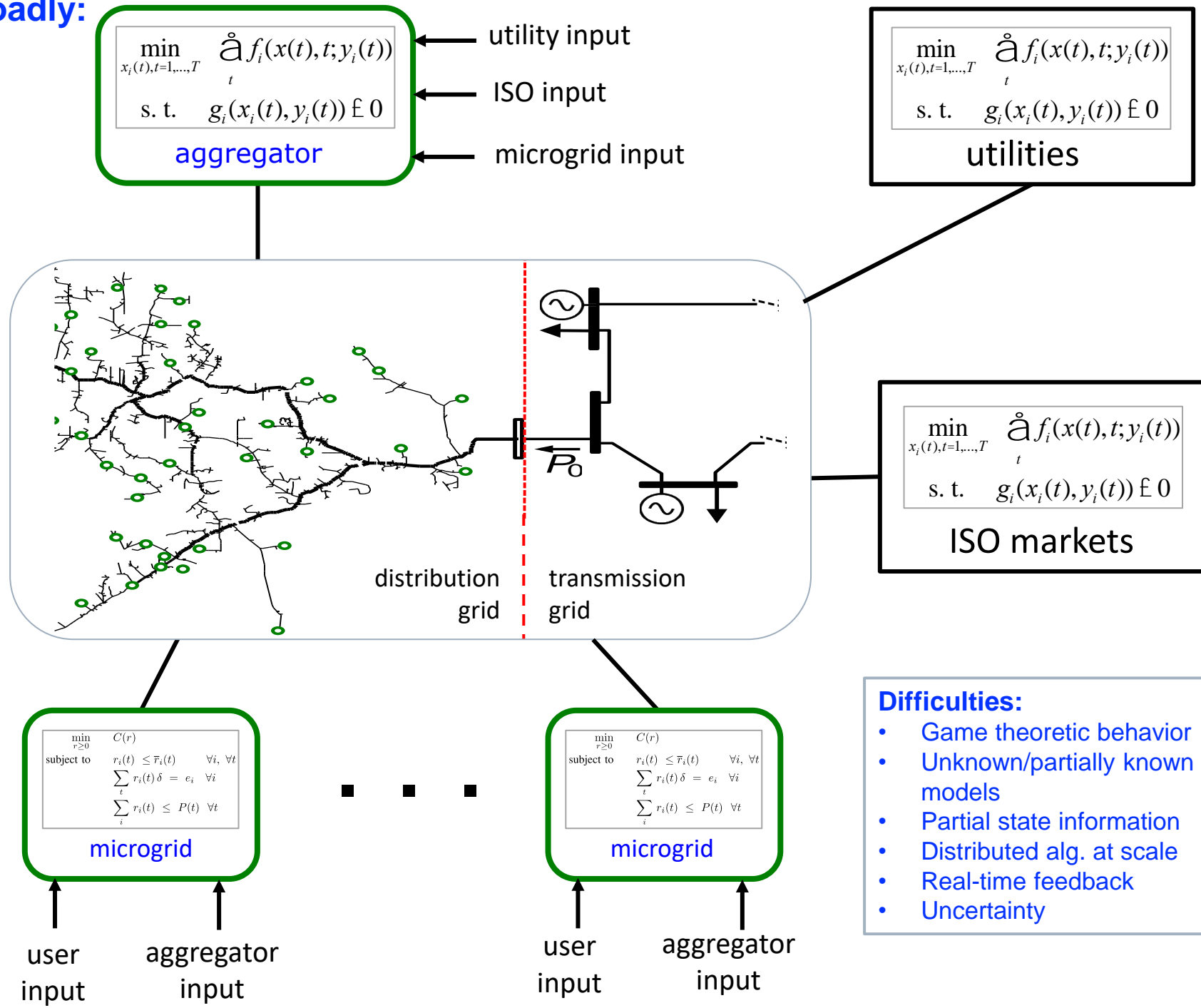
Can we identify  $Y$  from  $\bar{Y}$  for radial networks ?

**Theorem:** Yes ! [Yuan et al 2022]

Exactly recover both topology and impedances for radial nks  
 Constructive proof



More broadly:



- Difficulties:**
- Game theoretic behavior
  - Unknown/partially known models
  - Partial state information
  - Distributed alg. at scale
  - Real-time feedback
  - Uncertainty



# Lessons learnt

Most papers implicitly use single-phase models

- Balanced 3-phase systems have single-phase equivalents

Single-phase models applicable for many purposes

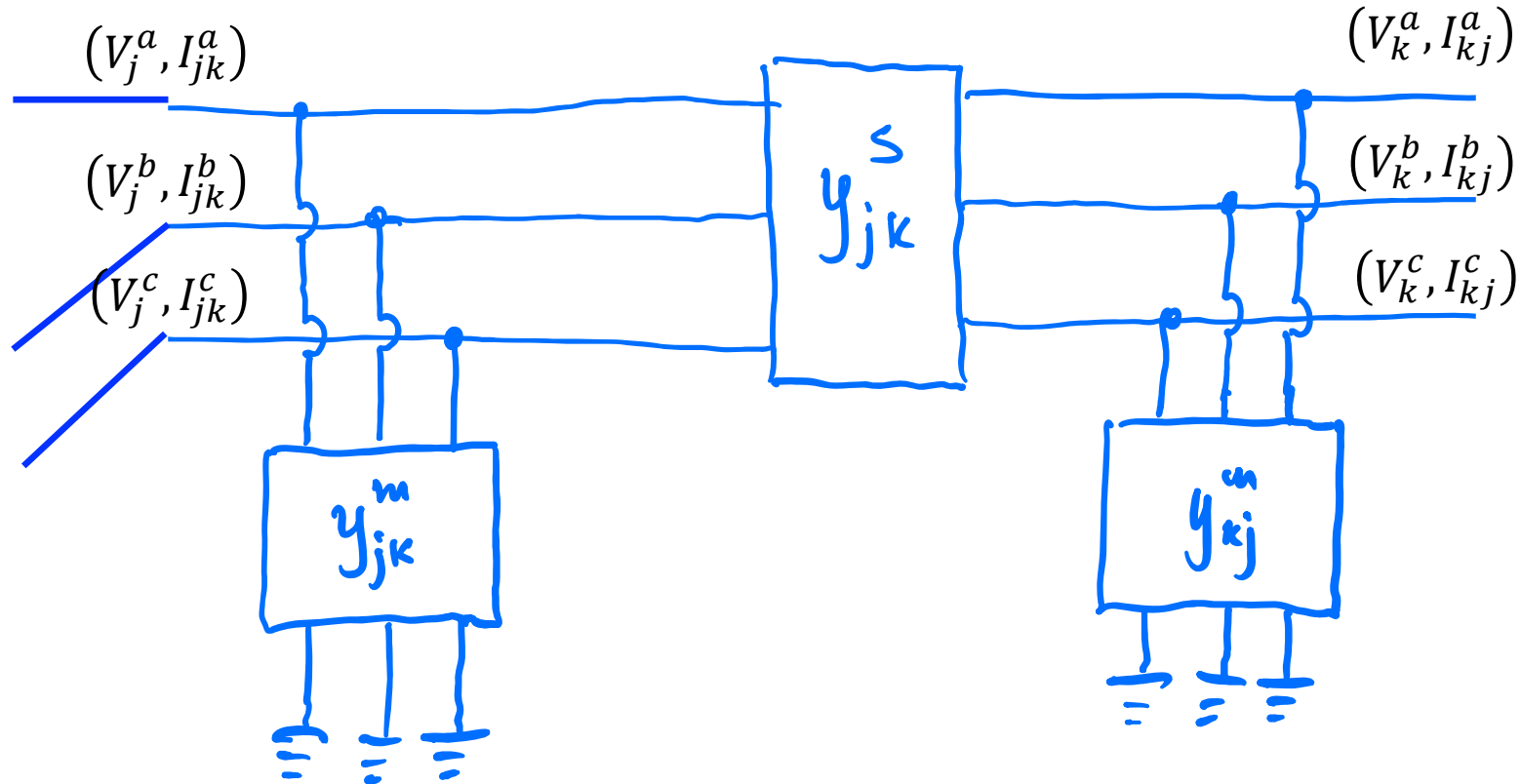
- Transmission system applications
- For illustrating **basic ideas** and analysis of most algorithms (unbalanced 3-phase models structurally similar to 1-phase models)

Unbalanced 3-phase modeling needed

- When control & optimization are explicitly on single-phase devices making up a 3-phase device
- For implementation in real systems when phases are not balanced



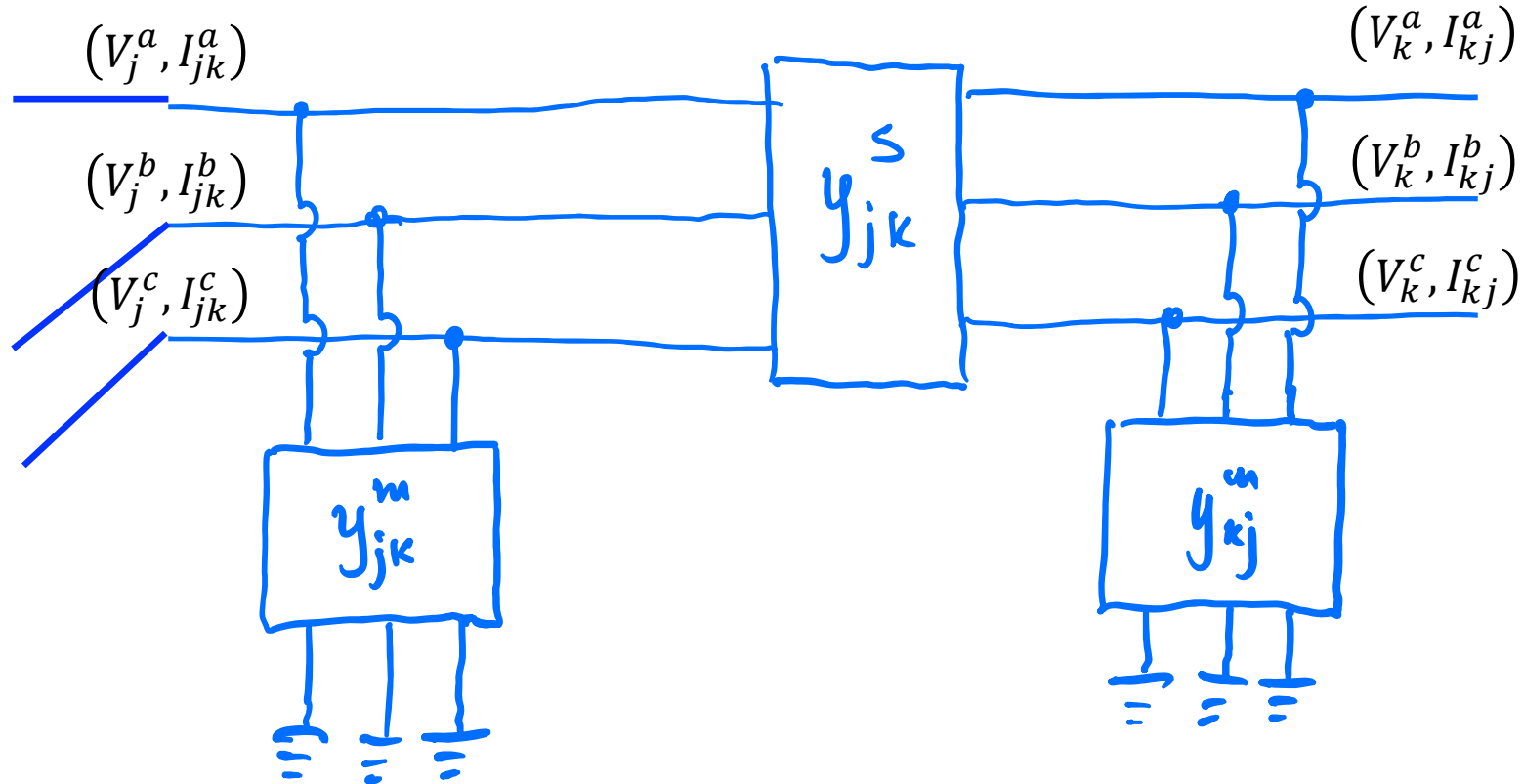
# Lessons learnt



- Many models assume **terminal** currents  $(I_{jk}^a, I_{jk}^b, I_{jk}^c)$  are controllable (optimization vars)
- Extension to 3-phase setting is straightforward



# Lessons learnt



$$I_{jk} = y_{jk}^s (V_j - V_k) + y_{jk}^m V_j$$

$$I_{kj} = y_{jk}^s (V_k - V_j) + y_{kj}^m V_k$$

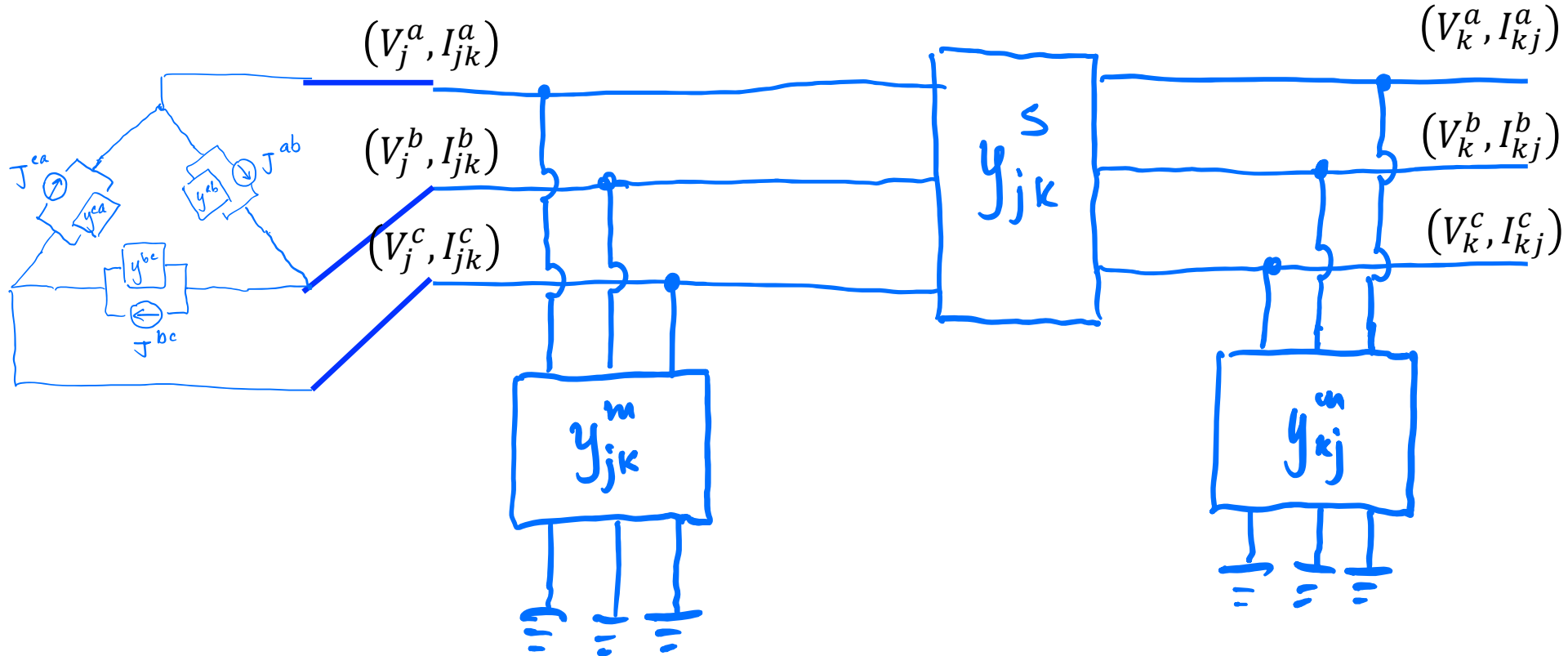
1-phase:  $I_{jk}, V_j^a \in \mathbb{C} \cdot y_{jk}^{s/m} \in \mathbb{C}$

3-phase:  $I_{jk}, V_j^a \in \mathbb{C}^3 \cdot y_{jk}^{s/m} \in \mathbb{C}^{3 \times 3}$





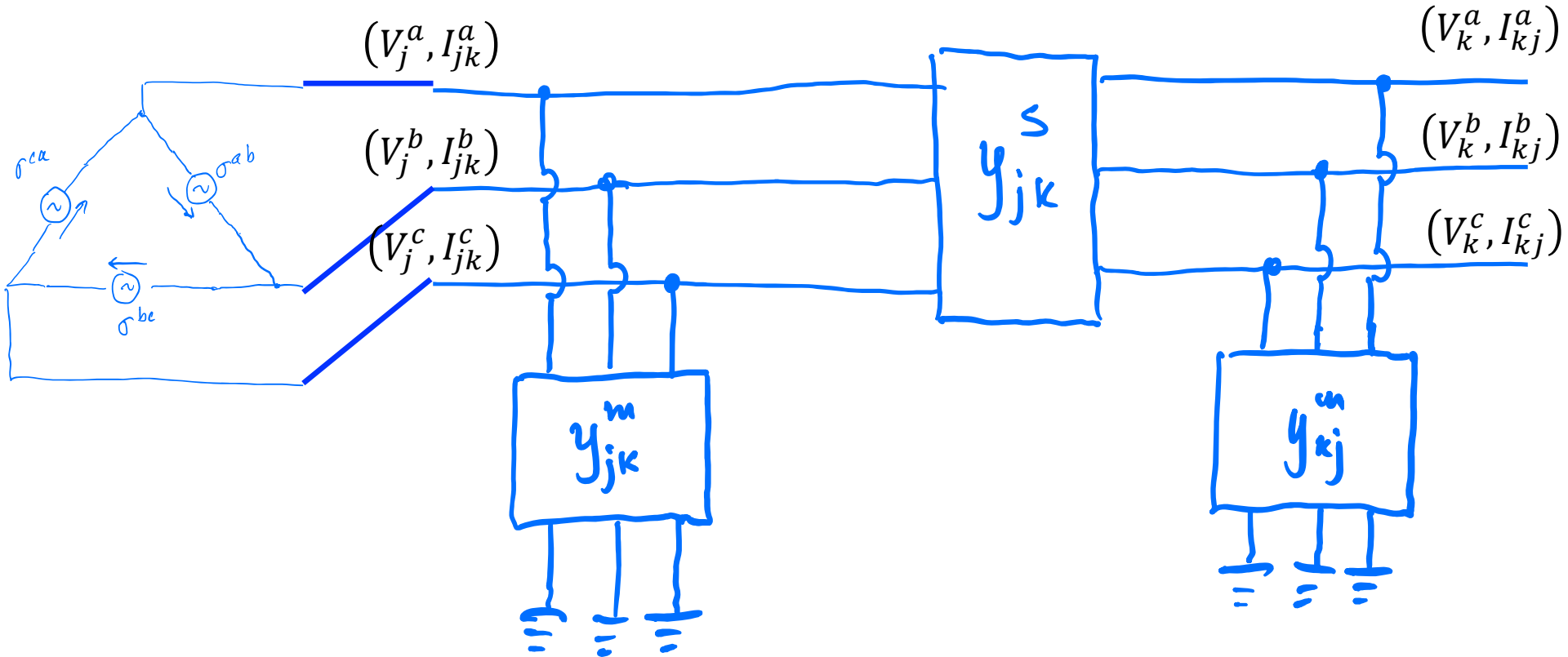
# Lessons learnt



- **Terminal** currents  $I_{jk}$  are externally observable, but often not directly controllable
- If only **internal** currents  $(J_j^{ab}, J_j^{bc}, J_j^{ca})$  of current sources are directly controllable, then need a 3-phase device model to convert between internal & terminal vars



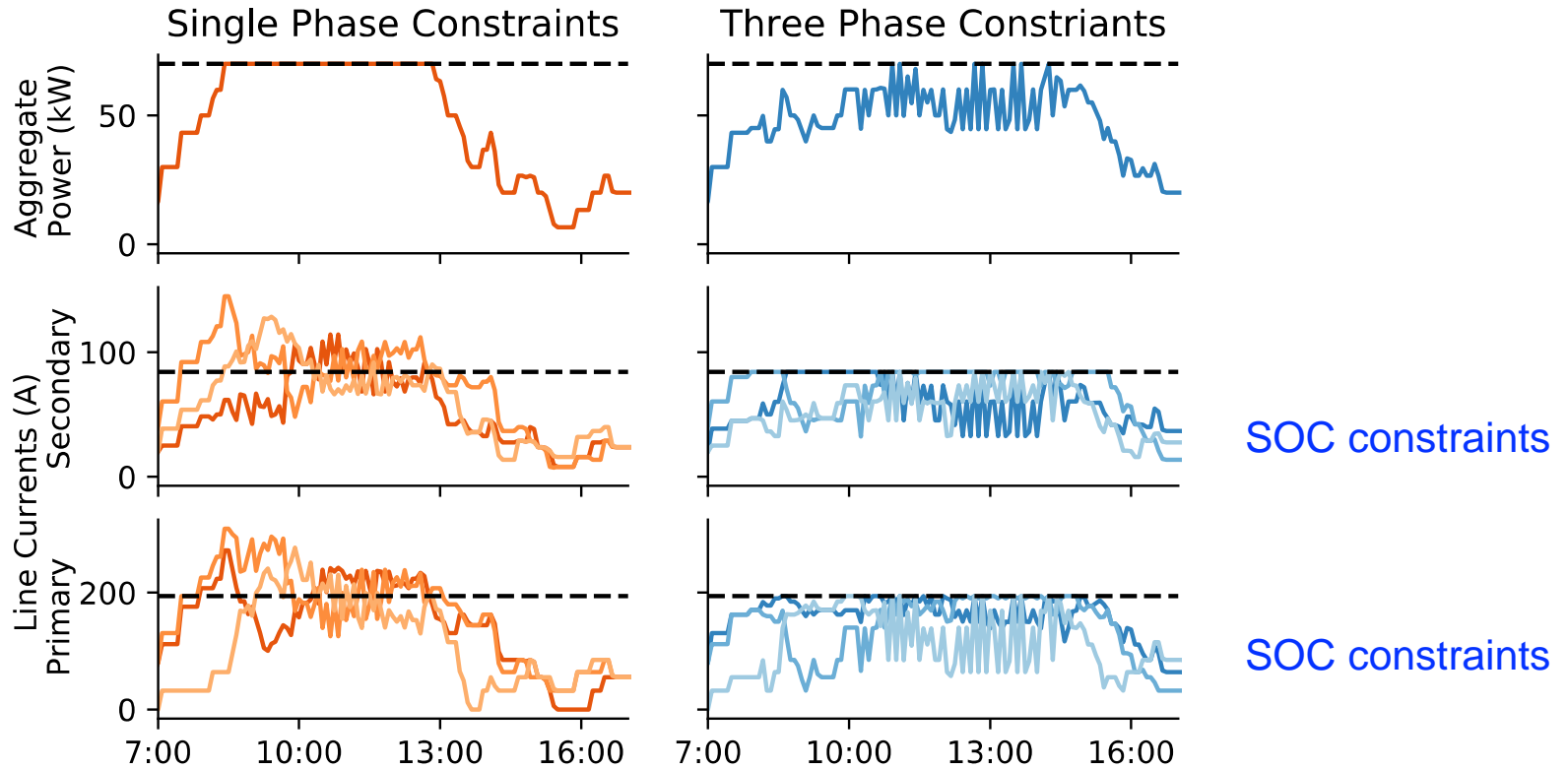
# Lessons learnt



Similarly for power sources or voltage sources



# Lessons learnt: example

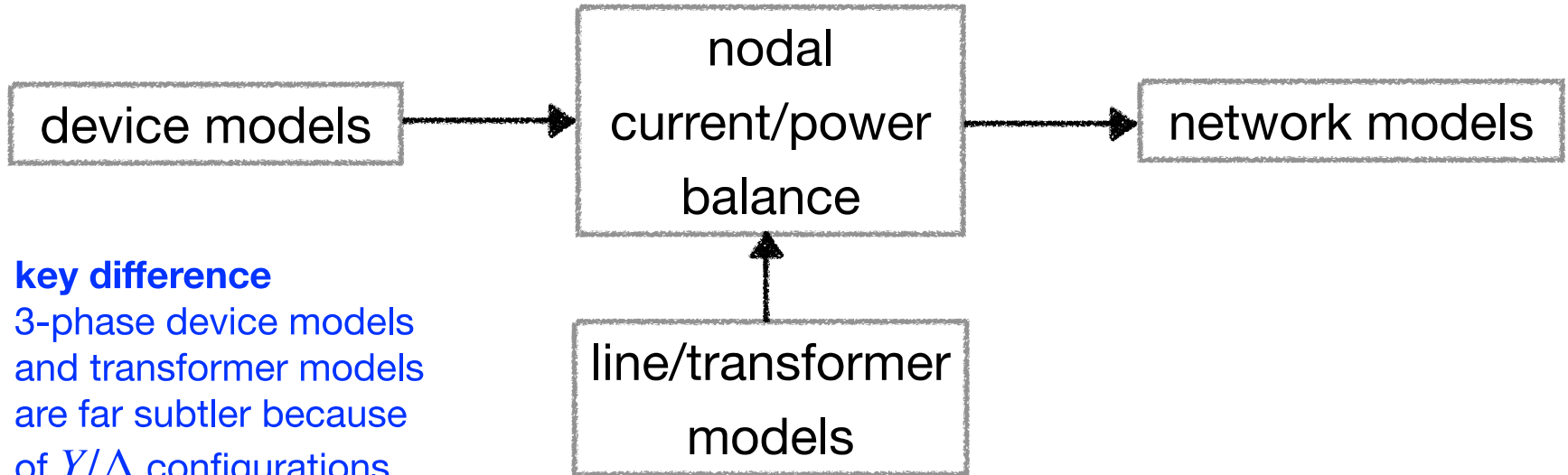


Left panel: Actual 3-phase currents violate capacity constraints if “single-phase constraints” are used (ACN-Sim based on Caltech ACN on Sept 5, 2018 data)

“single-phase constraints” :  $\sum_i r_i(t) \leq R$  (no phase line constraints for lack of phase info)



# Overview: 3-phase modeling



## key difference

3-phase device models and transformer models are far subtler because of  $Y/\Delta$  configurations

single-phase or 3-phase



# Key question

How to derive **external models** of 3-phase devices

1. Voltage/current/power sources, impedances (1-phase device: internal models)
2. ... in  $Y/\Delta$  configurations (conversion rules: int  $\rightarrow$  ext)
3. ... with or without neutral lines, grounded or ungrounded, zero or nonzero grounding impedances

Propose a simple and unified method to derive external models

Will use 3-phase voltage source in  $\Delta$  configuration to illustrate

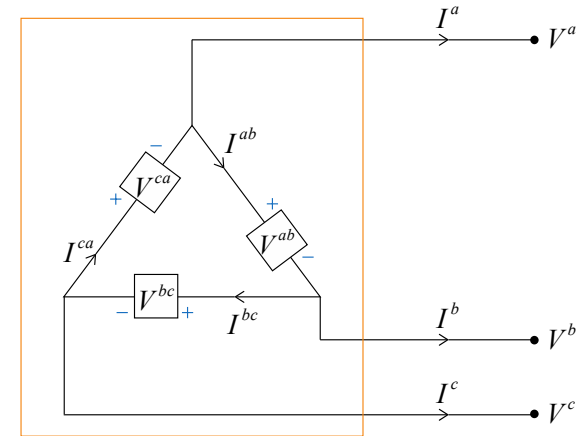


# Internal & terminal vars

## Internal vars ( $\Delta$ configuration)

Internal voltage, current, power across **single-phase** devices:

$$V^\Delta := \begin{bmatrix} V^{ab} \\ V^{bc} \\ V^{ca} \end{bmatrix}, I^\Delta := \begin{bmatrix} I^{ab} \\ I^{bc} \\ I^{ca} \end{bmatrix}, s^\Delta := \begin{bmatrix} s^{ab} \\ s^{bc} \\ s^{ca} \end{bmatrix} := \begin{bmatrix} V^{ab} \bar{I}^{ab} \\ V^{bc} \bar{I}^{bc} \\ V^{ca} \bar{I}^{ca} \end{bmatrix}$$



## Terminal vars

Terminal voltage, current, power (for both  $Y$  and  $\Delta$ ) **to reference**:

$$V := \begin{bmatrix} V^a \\ V^b \\ V^c \end{bmatrix}, I := \begin{bmatrix} I^a \\ I^b \\ I^c \end{bmatrix}, s := \begin{bmatrix} s^a \\ s^b \\ s^c \end{bmatrix} := \begin{bmatrix} V^a \bar{I}^a \\ V^b \bar{I}^b \\ V^c \bar{I}^c \end{bmatrix}$$

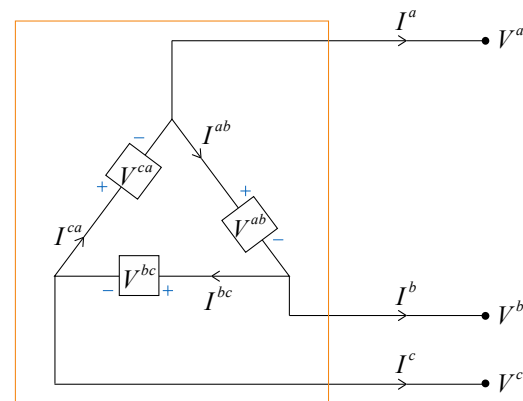
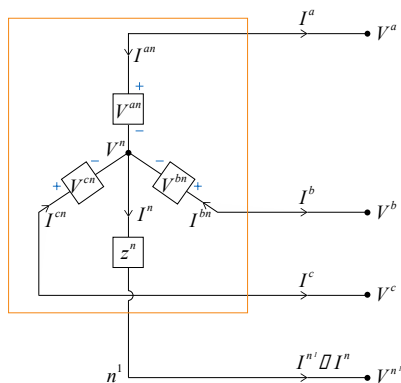
- $V$  is with respect to an arbitrary common reference point, e.g. the ground
- $I$  and  $s$  are in the direction **out** of the device



# Internal vs external model

1. External model = Internal model + Conversion rule

- External model: relation between  $(V, I, s)$
- Devices interact over network **only** through their terminal vars





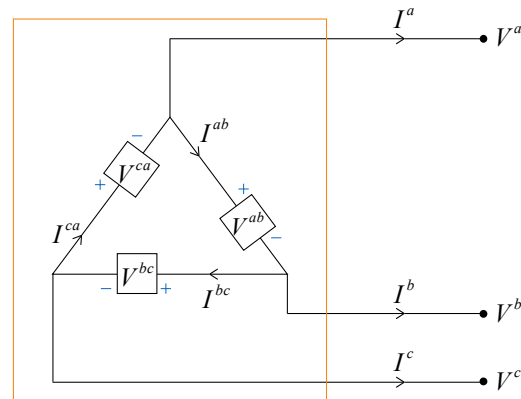
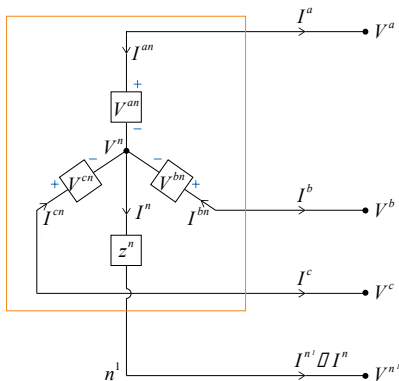
# Internal vs external model

1. **External model** = Internal model + Conversion rule

- External model: relation between  $(V, I, s)$
- Devices interact over network **only** through their terminal vars

2. **Internal model**: relation between  $(V^{Y/\Delta}, I^{Y/\Delta}, s^{Y/\Delta})$

- Independent of  $Y$  or  $\Delta$  configuration
- Depends only on behavior of single-phase devices
- Voltage/current/power source, impedance (voltage scr, ZIP load)

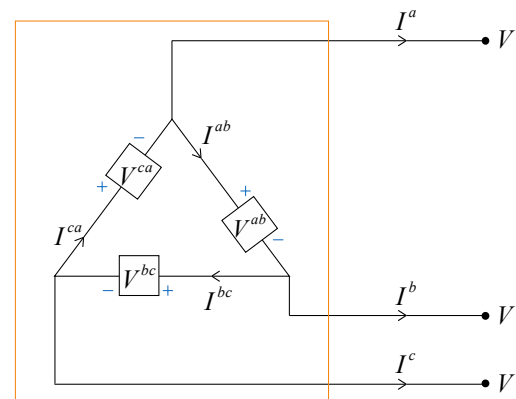
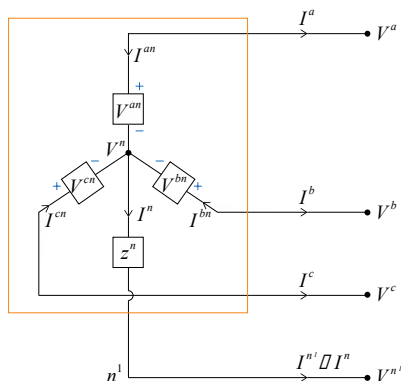






# Internal vs external model

1. **External model** = Internal model + Conversion rule
  - External model: relation between  $(V, I, s)$
  - Devices interact over network **only** through their terminal vars
2. **Internal model** : relation between  $(V^{Y/\Delta}, I^{Y/\Delta}, s^{Y/\Delta})$ 
  - Independent of  $Y$  or  $\Delta$  configuration
  - Depends only on behavior of single-phase devices
  - Voltage/current/power source, impedance (voltage scr, ZIP load)
3. **Conversion rule** : converts between internal and terminal vars
  - Depends only on  $Y$  or  $\Delta$  configuration
  - Independent of type of single-phase devices





# Conversion rule

## $\Delta$ configuration

Convert between **internal** vars and **external** vars

$$\begin{bmatrix} V_{ab} \\ V_{bc} \\ V_{ca} \end{bmatrix} = \underbrace{\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ -1 & 0 & 1 \end{bmatrix}}_{\Gamma} \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}, \quad \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = - \underbrace{\begin{bmatrix} 1 & 0 & -1 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}}_{\Gamma^T} \begin{bmatrix} I_{ab} \\ I_{bc} \\ I_{ca} \end{bmatrix}$$

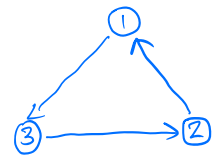
In vector form

$$\boxed{V^\Delta = \Gamma V, \quad I = -\Gamma^T I^\Delta}$$

↑
↑
↑
↑

internal voltage
terminal voltage
terminal current
internal current

$\Gamma$  is incidence matrix of:





# Conversion matrices $\Gamma$ & $\Gamma^T$

## Fortescue matrix $F$

Spectral decomposition:

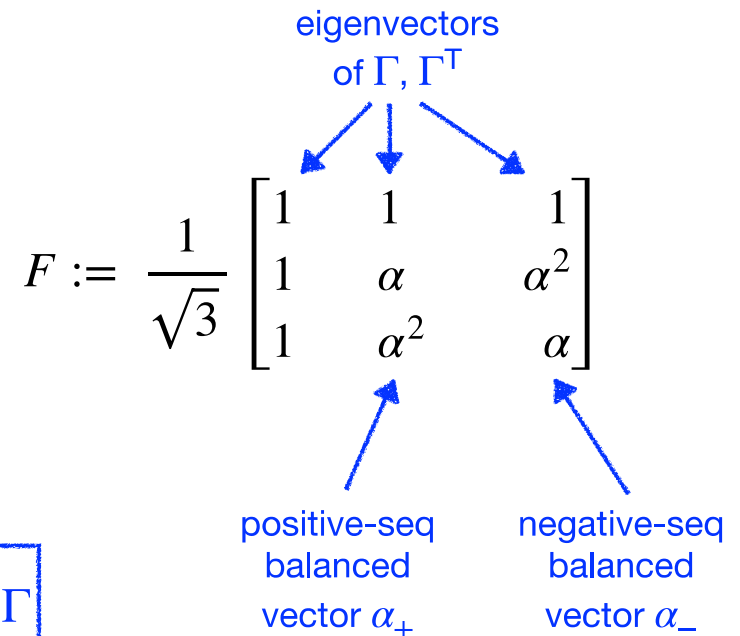
$$\Gamma = F\Lambda\bar{F}, \quad \Gamma^T = \bar{F}\Lambda F$$

where

$$\Lambda := \begin{bmatrix} 0 & & \\ & 1 - \alpha & \\ & & 1 - \alpha^2 \end{bmatrix},$$

and  $\alpha := e^{-i2\pi/3}$

Pseudo-inverses:  $\Gamma^\dagger = \frac{1}{3}\Gamma^T, \quad \Gamma^{T\dagger} = \frac{1}{3}\Gamma$



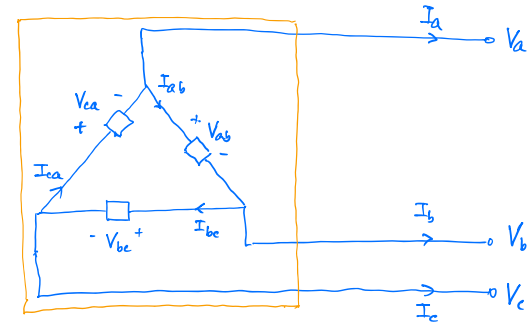


# Conversion rule

## $\Delta$ configuration

1. Converts between internal and terminal voltages & currents

$$V^\Delta = \Gamma V, \quad I = -\Gamma^\top I^\Delta$$





# Conversion rule

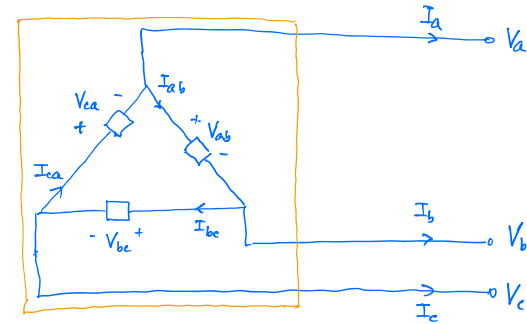
## $\Delta$ configuration

1. Converts between internal and terminal voltages & currents

$$V^\Delta = \Gamma V, \quad I = -\Gamma^T I^\Delta$$

2. Given  $V^\Delta$ : terminal voltage  $V = \frac{1}{3} \Gamma^T V^\Delta + \gamma \mathbf{1}$ ,  $\gamma \in \mathbb{C}$

•  $\gamma := \frac{1}{3} \mathbf{1}^T V$ : zero-sequence terminal voltage (fixed by reference voltage)





# Conversion rule

## $\Delta$ configuration

1. Converts between internal and terminal voltages & currents

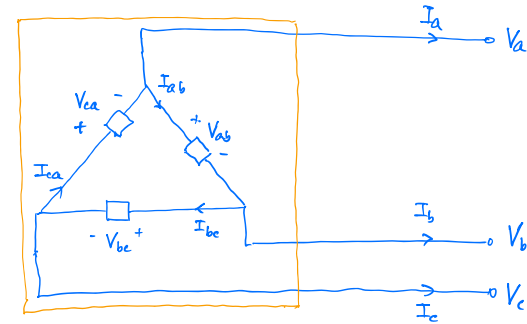
$$V^\Delta = \Gamma V, \quad I = -\Gamma^T I^\Delta$$

2. Given  $V^\Delta$ : terminal voltage  $V = \frac{1}{3} \Gamma^T V^\Delta + \gamma \mathbf{1}$ ,  $\gamma \in \mathbb{C}$

•  $\gamma := \frac{1}{3} \mathbf{1}^T V$ : zero-sequence terminal voltage (fixed by reference voltage)

3. Given  $I$ : internal current  $I^\Delta = -\frac{1}{3} \Gamma I + \beta \mathbf{1}$ ,  $\beta \in \mathbb{C}$

•  $\beta := \frac{1}{3} \mathbf{1}^T I^\Delta$ : zero-sequence internal current (does not affect terminal current)





# Conversion rule

## $\Delta$ configuration

1. Converts between internal and terminal voltages & currents

$$V^\Delta = \Gamma V, \quad I = -\Gamma^T I^\Delta$$

2. Given  $V^\Delta$ : terminal voltage  $V = \frac{1}{3} \Gamma^T V^\Delta + \gamma \mathbf{1}$ ,  $\gamma \in \mathbb{C}$

•  $\gamma := \frac{1}{3} \mathbf{1}^T V$ : zero-sequence terminal voltage (fixed by reference voltage)

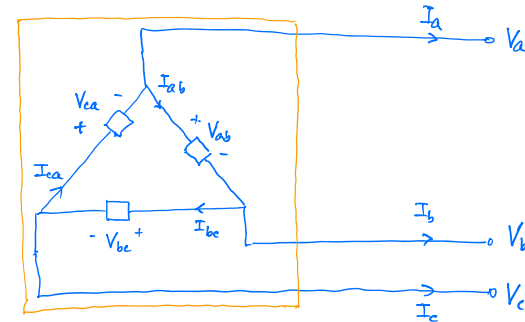
3. Given  $I$ : internal current  $I^\Delta = -\frac{1}{3} \Gamma I + \beta \mathbf{1}$ ,  $\beta \in \mathbb{C}$

•  $\beta := \frac{1}{3} \mathbf{1}^T I^\Delta$ : zero-sequence internal current (does not affect terminal current)

4. Relation between  $s$  and  $s^\Delta$  through  $(V, I^\Delta)$ :

$$s = -\text{diag}(VI^{\Delta H}\Gamma), \quad s^\Delta = \text{diag}(\Gamma VI^{\Delta H})$$

(no direct relation between  $s$  and  $s^\Delta$ )





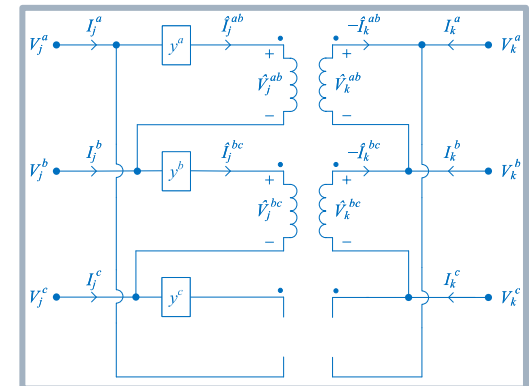
# Example: transformers

**Theorem 1.** *The external models of three-phase transformers in  $YY$ ,  $\Delta\Delta$ ,  $\Delta Y$  and  $Y\Delta$  configurations take the form*

$$I = D^T Y_{YY} D (V - \gamma)$$

where

$$\begin{array}{ll}
 YY : & D := \begin{bmatrix} \mathbb{I} & 0 \\ 0 & \mathbb{I} \end{bmatrix} \\
 \Delta\Delta : & D := \begin{bmatrix} \Gamma & 0 \\ 0 & \Gamma \end{bmatrix} \\
 \Delta Y : & D := \begin{bmatrix} \Gamma & 0 \\ 0 & \mathbb{I} \end{bmatrix} \\
 Y\Delta : & D := \begin{bmatrix} \mathbb{I} & 0 \\ 0 & \Gamma \end{bmatrix}
 \end{array}$$



unified & modular characterization





# Overall model: device + network

1. **Network model** relates terminal vars  $(V, I, s)$ 
  - Nodal current balance (**linear**):  $I = YV$
  - Nodal power balance (**nonlinear**):  $s_j = \sum_{k:j \sim k} \text{diag} \left( V_j (V_j - V_k)^H y_{jk}^{sH} + V_j V_j^H y_{jk}^{mH} \right)$
  - Either can be used
2. **Device model** for each 3-phase device
  - Internal model  $\left( V_j^{Y/\Delta}, I_j^{Y/\Delta}, s_j^{Y/\Delta}, \gamma_j, \beta_j \right)$  + conversion rules
  - External model  $\left( V_j, I_j, s_j, \gamma_j, \beta_j \right)$  with internal parameters
  - Either can be used
  - Power source models are nonlinear; other devices are linear



# Unbalance 3-phase modeling

## **Power System Analysis**

### **A Mathematical Approach**

**Steven H. Low**

DRAFT available at: <http://netlab.caltech.edu/book/>

Corrections, questions, comments appreciated!



# Backup slides



# Why Caltech

## Caltech energy system is large & complex

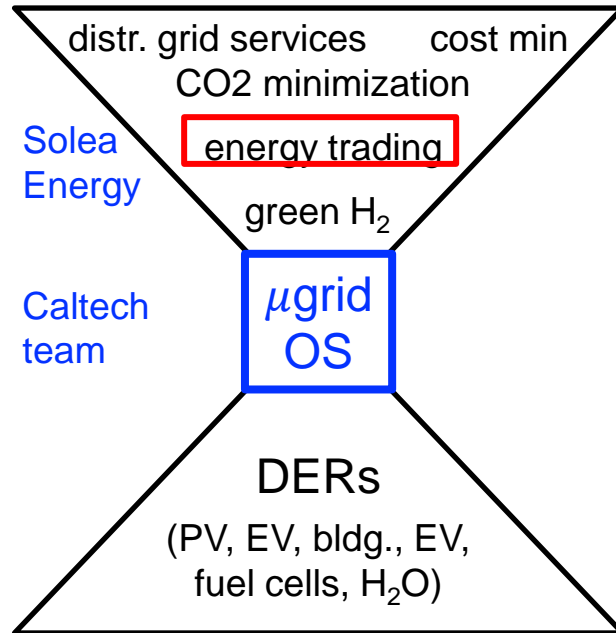
- Energy needs of ~5,000 population correspond to ~20,000 people (CA), peak (electric): 20MW [Caltech Facilities, 2021]
- Stanford: 30K population correspond to 33,000 households (CA); peak (integrated energy system): 40MW [de Chalendar et al, 2019]
- More technical challenges to overcome
- Invaluable live testbed for R&D and validation

## Caltech system is representative of large campuses

- With district heating and cooling systems (more popular in EU, China, Russia, Japan)
- e.g., Stanford, PNNL (both pursuing campus decarbonization)
- Stanford's integrated system: first-of-a-kind [de Chalendar et al, 2019]



# Example path



We need to develop interfaces

- With Facilities: DER
- With Solea Energy: trading

## Warehouses

- Consumes 6 kWh/sqft-year, but can generate 90 kWh/sqft-year of PV
- US has 10B sqft of warehouse space
- Can generate 100 GW PV (~10% of total 1TW of US rooftop PV capacity)
- \$6B/year annual electricity cost
- \$150B microgrid infrastructure market (\$15M / 1M sqft warehouse)

## Value proposition

- DER opt technology can save 10% of annual electricity cost (\$600M/year)
- ... and 2% of capital cost (\$3B)
- Emission reduction by 80-100%

Co-PI on Solea led DoE GRIP proposal (submitted March 2023)